

**MATHEMATICS**  
**Monday October 17 2016**  
**Fourth Exercise Class**

- 1) Verify that  $a_n = 3 - \frac{1}{n^2+1}$  approaches  $L = 3$  for  $n \rightarrow +\infty$ .
- 2) Verify that  $a_n = (-1)^n$  does not admit limit.
- 3) Verify whether the sequence  $a_n = \left(-\frac{1}{n}\right)_{n=1}^{\infty}$  is bounded from below, bounded from above, or bounded.
- 3) Verify whether the sequence  $a_n = \left(1 - n^2\right)_{n=1}^{\infty}$  is bounded from below, bounded from above, or bounded.
- 4) Study domain, sign and axis-intercepts of the following functions
  - $y = \frac{5 \cos x}{1+2 \cos x}$
  - $y = \frac{\ln x}{\sqrt{1+\cos x}}$
  - $y = \frac{\ln(|\sin x + \cos x|)}{3^{2 \sin x} - 4 \cdot 3^{\sin x} + 3}$
  - $y = \frac{\ln(1 - \sin^2 x)}{x e^{\sin x}}$
  - $y = \frac{\log(1+x^2)}{\sin x - x}$