

# BAE Math 2 Exercise

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November 23 2023

## Exercise 1.

Given the matrices  $\mathbf{A}$  e  $\mathbf{B}$  where:

$$\mathbf{A} = \begin{pmatrix} 1 & 0 & 3 \\ 8 & 2 & 6 \\ 4 & 1 & 5 \end{pmatrix} \quad \mathbf{B} = \begin{pmatrix} 5 & 1 & 0 \\ 0 & 2 & 1 \\ 5 & 3 & 6 \end{pmatrix}$$

evaluate  $A + B$ ,  $A^T$ ,  $C = 4A$ .

## Exercise 2.

Given the following matrices

$$\mathbf{A} = \begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix} \quad \mathbf{B} = \begin{pmatrix} 2 & 1 \\ -1 & 1 \end{pmatrix} \quad \mathbf{C} = \begin{pmatrix} 0 & 2 \\ -2 & 1 \end{pmatrix},$$

evaluate:

- $2A - B$ ;
- $3A + 2B - 4C$ ;
- $-2A + B + 2C - 2B$ ;
- $3B + 2(2A - C) - (A + B + 2C)$ .

**Exercise 3.** Given the following matrices

$$\mathbf{A} = \begin{pmatrix} 1 & -1 & 0 \\ -1 & 1 & 1 \end{pmatrix} \quad \mathbf{B} = \begin{pmatrix} -2 & 1 & -1 \\ 2 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix} \quad \mathbf{C} = \begin{pmatrix} 0 & 1 \\ 1 & 1 \\ 0 & -1 \end{pmatrix},$$

evaluate, when possible:

- $A \cdot B$ ;
- $(B \cdot B) \cdot A$ ;
- $B + (C \cdot A)$ ;
- $B \cdot A$ ;
- $B \cdot A^T$ ;
- $A^T + B \cdot C$ .

**Exercise 4.**

Evaluate the determinants of the following matrices

$$A = \begin{pmatrix} 2 & 3 \\ 1 & -2 \end{pmatrix}; \quad B = \begin{pmatrix} -11 & 3 \\ 2 & 0 \end{pmatrix}; \quad C = \begin{pmatrix} 2 & 3 & -2 \\ 1 & -2 & 0 \\ 0 & -1 & 2 \end{pmatrix};$$

$$D = \begin{pmatrix} 2 & -2 & -2 \\ 1 & 1 & 0 \\ -3 & 4 & 0 \end{pmatrix}; \quad E = \begin{pmatrix} 7 & 0 & 0 \\ 1 & 1 & 0 \\ -3 & 4 & -3 \end{pmatrix}; \quad F = \begin{pmatrix} 1 & -4 & 2 \\ 0 & 2 & -1 \\ 0 & 0 & 5 \end{pmatrix};$$

$$G = \begin{pmatrix} -2 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 3 \end{pmatrix}; \quad H = \begin{pmatrix} 1 & 2 & 2 & 3 \\ 4 & 1 & -1 & 2 \\ 3 & 6 & 6 & 8 \\ 3 & 2 & 1 & 3 \end{pmatrix}.$$

**Exercise 5.**

When possible evaluate the inverse of the following matrices

$$A = \begin{pmatrix} 1 & 2 \\ 2 & -1 \end{pmatrix} \quad B = \begin{pmatrix} 1 & -4 & 2 \\ 0 & 2 & -1 \\ 0 & 0 & 5 \end{pmatrix} \quad C = \begin{pmatrix} 1 & -1 & 3 \\ 1 & 1 & 2 \\ 2 & 0 & 7 \end{pmatrix}$$

**Exercise 6.**

Let  $A$  be the following matrix

$$A = \begin{pmatrix} 1 & k & 0 \\ 0 & 1 & k-4 \\ 2 & k & 0 \end{pmatrix}$$

- establish for which value of  $k$  the matrix  $A$  is invertible;
- for the  $k$  values of the question a), determine the inverse of  $A$ .

**Exercise 7.**

Given the matrix  $A$

$$A = \begin{pmatrix} 2 & 0 & 5 \\ -4k & 4k-1 & k-2 \\ 0 & 1-4k & 0 \end{pmatrix}$$

are there values for  $k$  such that the matrix is invertible?.

**Exercise 8.**

Given the matrices

$$A = \begin{pmatrix} 1 & 1 \\ 2 & 3 \end{pmatrix}, \quad B = \begin{pmatrix} 1 & 3 \\ 0 & 1 \end{pmatrix},$$

verify the property

$$(A \cdot B)^{-1} = B^{-1} \cdot A^{-1}.$$

Moreover verify that

$$(A^T)^{-1} = (A^{-1})^T.$$