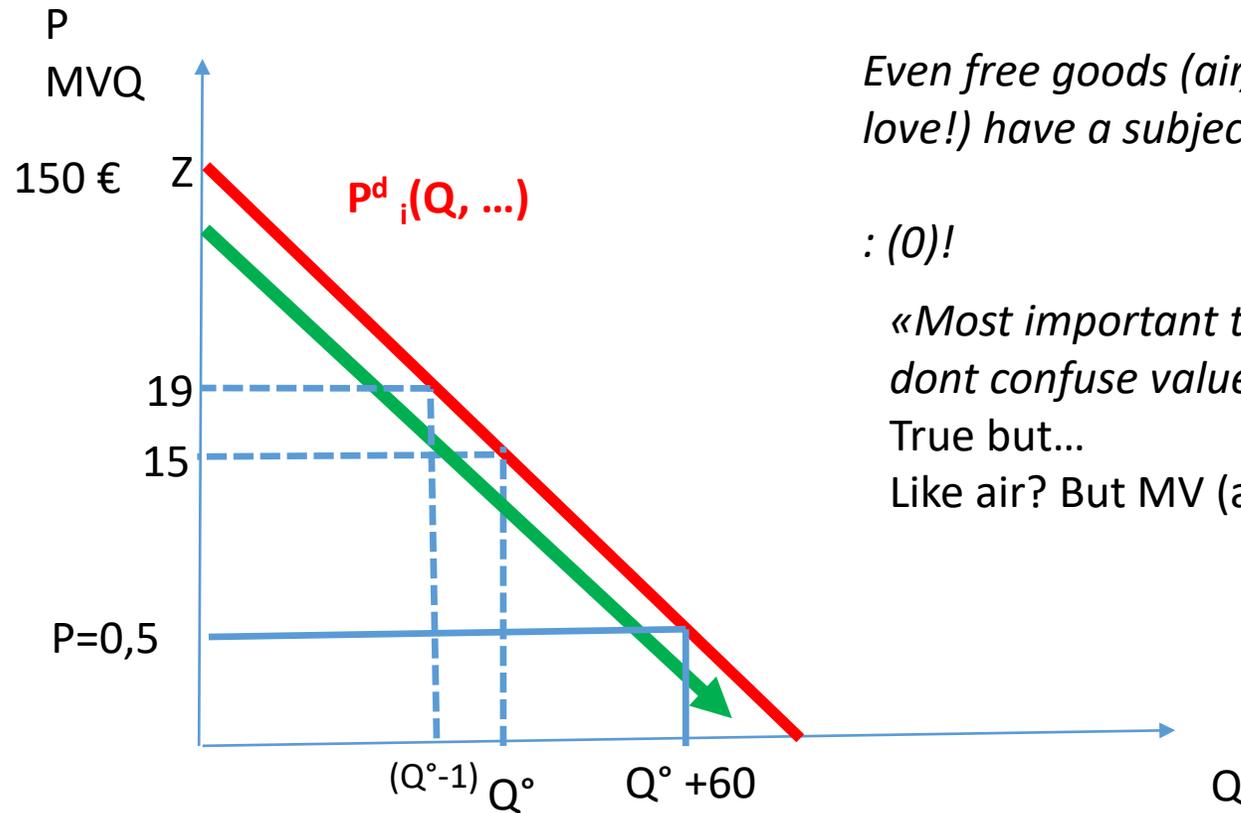




# Decreasing demand curves



*Even free goods (air, company-cleaned car, not love!) have a subjective Marginal Value = price ...*

*: (0)!*

*«Most important things in life have no price: dont confuse value and price»*

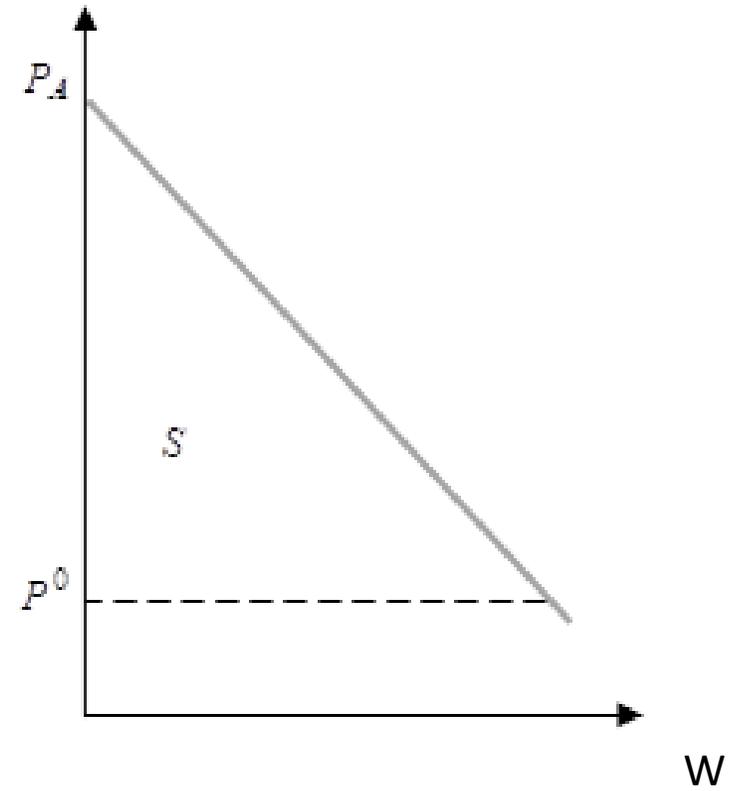
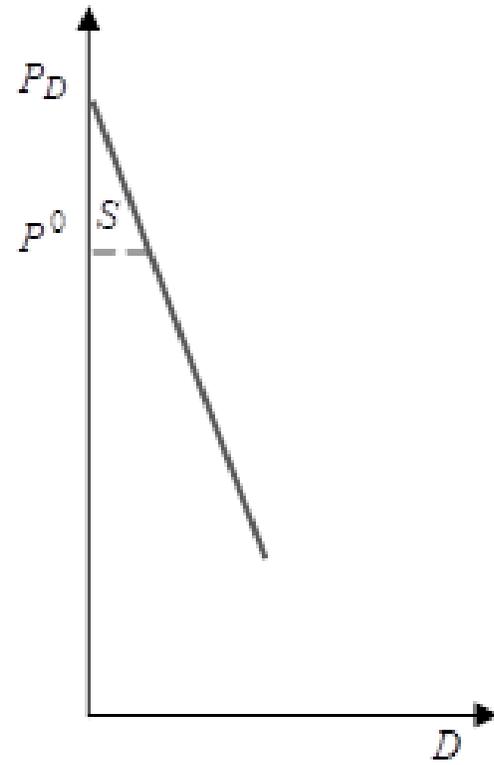
*True but...*

*Like air? But MV (air) = ... zero*

$Q^{\text{th}}$



# The surplus practice: Diamonds and Water



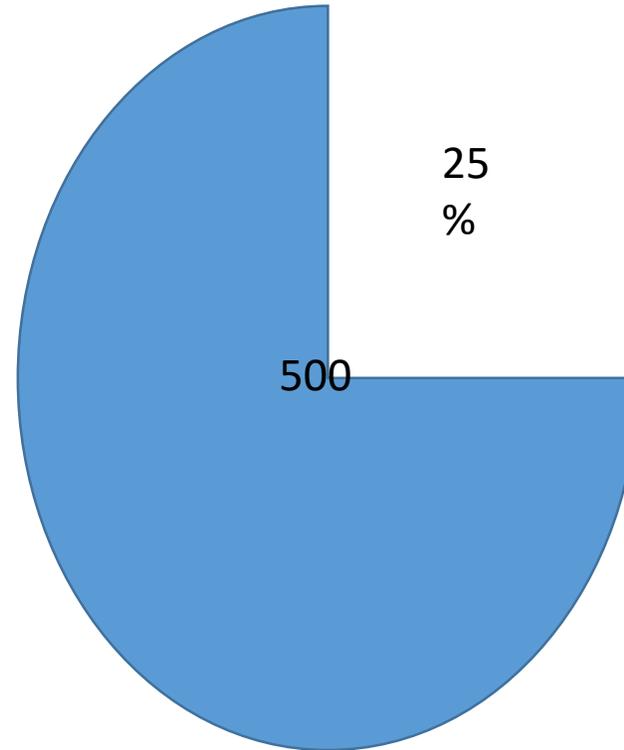
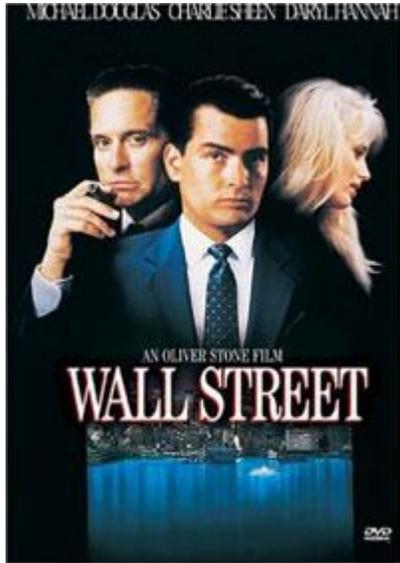


# Chapter 4

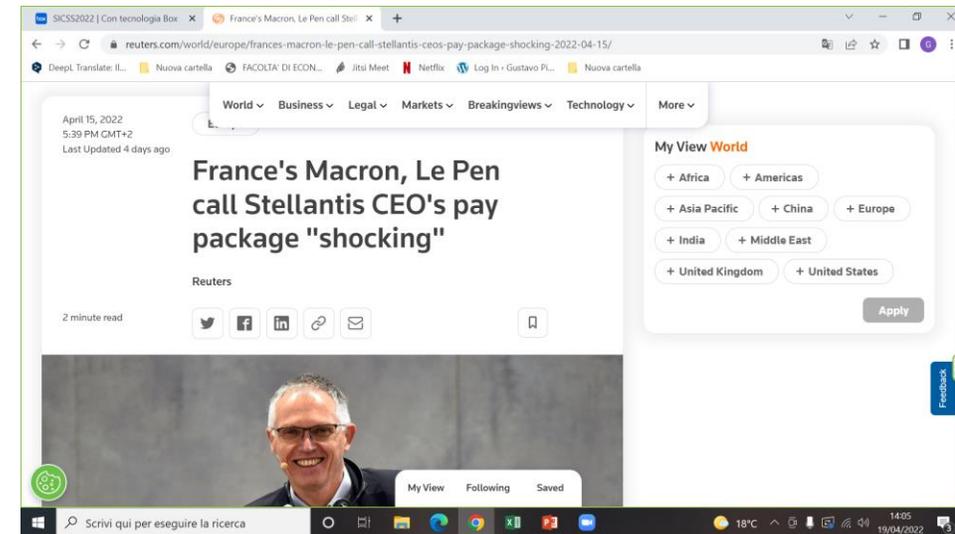
$Q^*$  such that:

$$\text{Max } \Pi (Q) = P(Q) Q - TC (Q)$$

Really?



Mr. Stock Option,  
Sundar Pichai



$$\text{Max}_Q \Pi(Q) = TR(Q) - TC(Q)$$

$Q^*$  such that

$$\frac{\delta TR(Q^*)}{\delta Q} - \frac{\delta TC(Q^*)}{\delta Q} = 0$$

$$\text{MgR}(Q^*) = \text{MgC}(Q^*)$$

$$TC(Q) \equiv \min TC(Q)$$

If  $MgR(13) = 240 \text{ €}$  and  $MgC(13) = 200 \text{ €}$  and  
 $\Pi(13) = 3450 \text{ €}$  ...

$$\begin{aligned}\Pi(14) &= \dots ? \\ &= 3490 \text{ €}\end{aligned}$$

If  $MgR(100) = 10 \text{ €}$  and  $MgC(100) = 12 \text{ €}$  and  
 $\Pi(100) = 3450 \text{ €}$  ...

$$\begin{aligned}\Pi(99) &= \dots ? \\ &= 3452 \text{ €}\end{aligned}$$

The value of everything that the entrepreneur has to give up to, for the production of that specific quantity, i.e. for gauging whether to be an entrepreneur.

Not just how much and how, but

**IF**

to produce: if  $[Q^s(P) > 0]$ .

- a) 25.000 euro per year with no effort to teach my lectures.
- b) As an entrepreneur I earn revenue equal to 50.000 euro from my business and need to pay 30.000 euro to my employees.

In our example 25.000 euro is the “normal profit” of the entrepreneur, i.e. the profit that can be obtained in the best available possible alternative (in this case the professor activity).

The normal profit is thus an opportunity cost for the entrepreneur that desires to launch a new activity.

Let us define economic profit (such that, if positive, leads to become an entrepreneur):

$$\begin{aligned}\text{Economic Profit} &= \text{Total Revenues} - \text{Total Opportunity Costs} \\ &= \text{Total Revenues} - (\text{Normal Profits} + \text{All Other Opportunity Costs})\end{aligned}$$

In our example, economic profit is equal to? And what if revenues were to equal 55.000 euro?  
-5000;0

**Economic Profit > 0 ?**

**Total Revenues – Total Remaining Opportunity Costs > Normal Profits**

$$50.000 - 30.000 < 25.000 \quad 55.000 - 30.000 = 25.000$$

Economic Profits  $> 0$

Total Revenues – (Normal Profits + Total Remaining Opportunity Costs)  $> 0$

Total Revenues – Total Remaining Opportunity Costs  $>$  Normal Profits

Economic Profits  $> 0$



Extraprofits!

Revenues = 100.000 euro

Employees Costs = 40.000 euro

Ownership of office building that could be rented at 10.000 euro. Normal profits baby-sitting friends' kids 50.000 euro.

Economic profits?

$[100.000 - 40.000 - 10.000 - 50.000] = 0.$

No extra-profits

Revenues = 200.000 euro.

Employees costs = 180.000 euro.

*Renting of garage = 30.000 euro*

**SUNK COST**

*Independently of whether I stay in the market or not as an entrepreneur, having already subscribed a location contract.*

Accounting profit?

-10.000 €

Economic Profit?

+20.000 € (lower losses compared to not being an entrepreneur)

1) How much to produce and 2)  
how to produce it

Always together, never separate:  
max  $\Pi$  and min TC (but be aware!)

We will separate them, ever so  
briefly.

# How to Produce? The realm of engineers



The production process consists on the use and combination of resources (also called **inputs** or production factors) aimed at creating a new resource (also called **output**).

Output (Y) has a temporal dimension: 10 units per hour, week, year, etc. That is, the output is a **flow**.

Similarly for the inputs (X, either K or L).

For the raw materials - consumed entirely in the production process - used in the production process, 100 tons of steel (or, in the future, polypropylene) are used per day to produce Y Fiat per day in that factory.

For capital (also called K) such as machines that are not consumed entirely in the production process, we will talk about the services per unit of time provided by the machine: a tractor is used for X machine-hours per day, per week, per year. We will call the **production capacity** of a durable good the maximum amount of services for production that can potentially be obtained from it in each period.

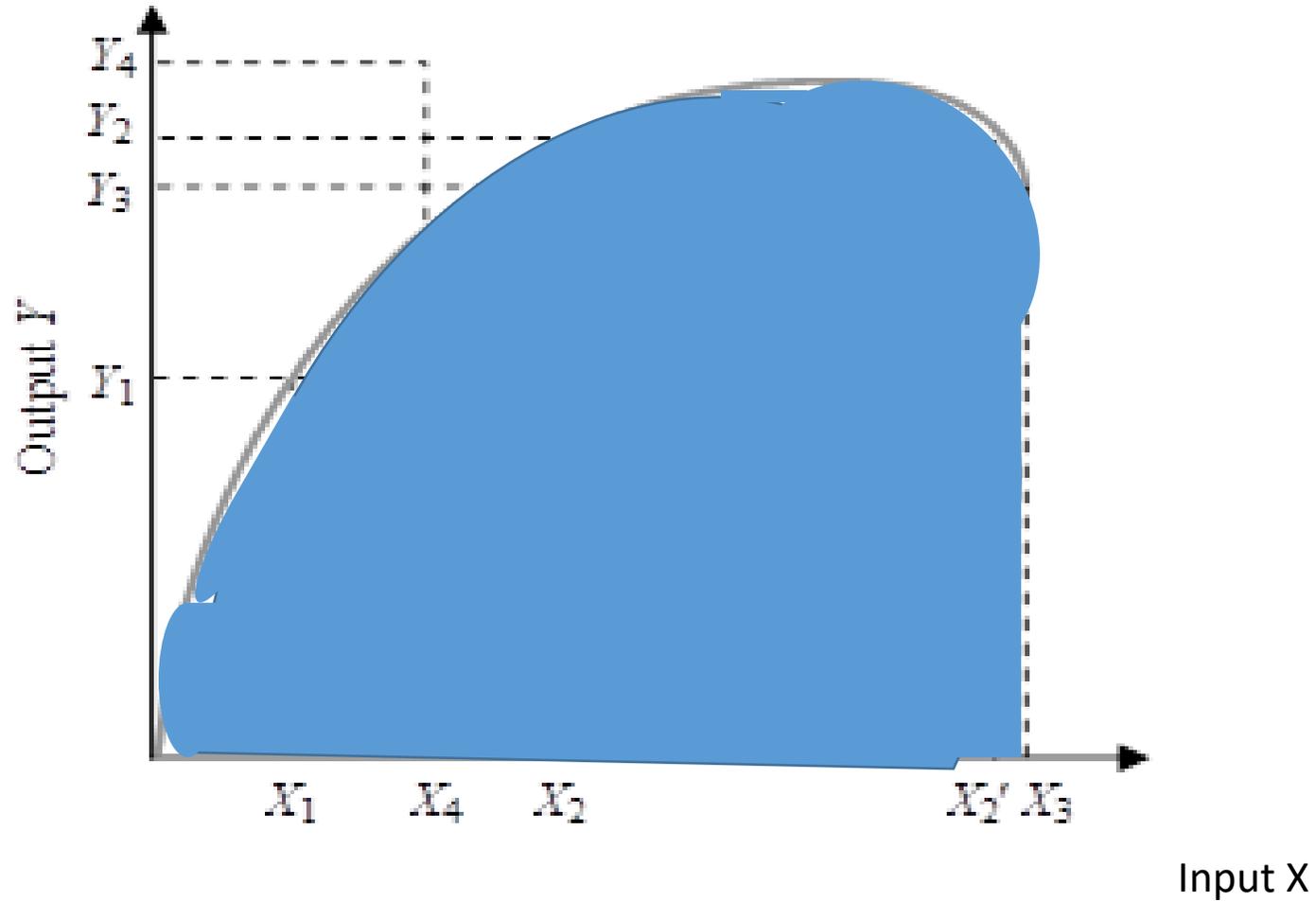
Similarly, for labor (L) factor services we will talk about hours worked per day, per week, per month, etc.

**No guns!**  
**Both against**  
**consumers and**  
**factors of**  
**production.**  
**Constraint n. 1**

There are different ways of transforming an input or a combination of inputs in an output: the relationship (between) all **available** input and output combinations to the entrepreneur is called "**technology**", her/his "science" or ... art.

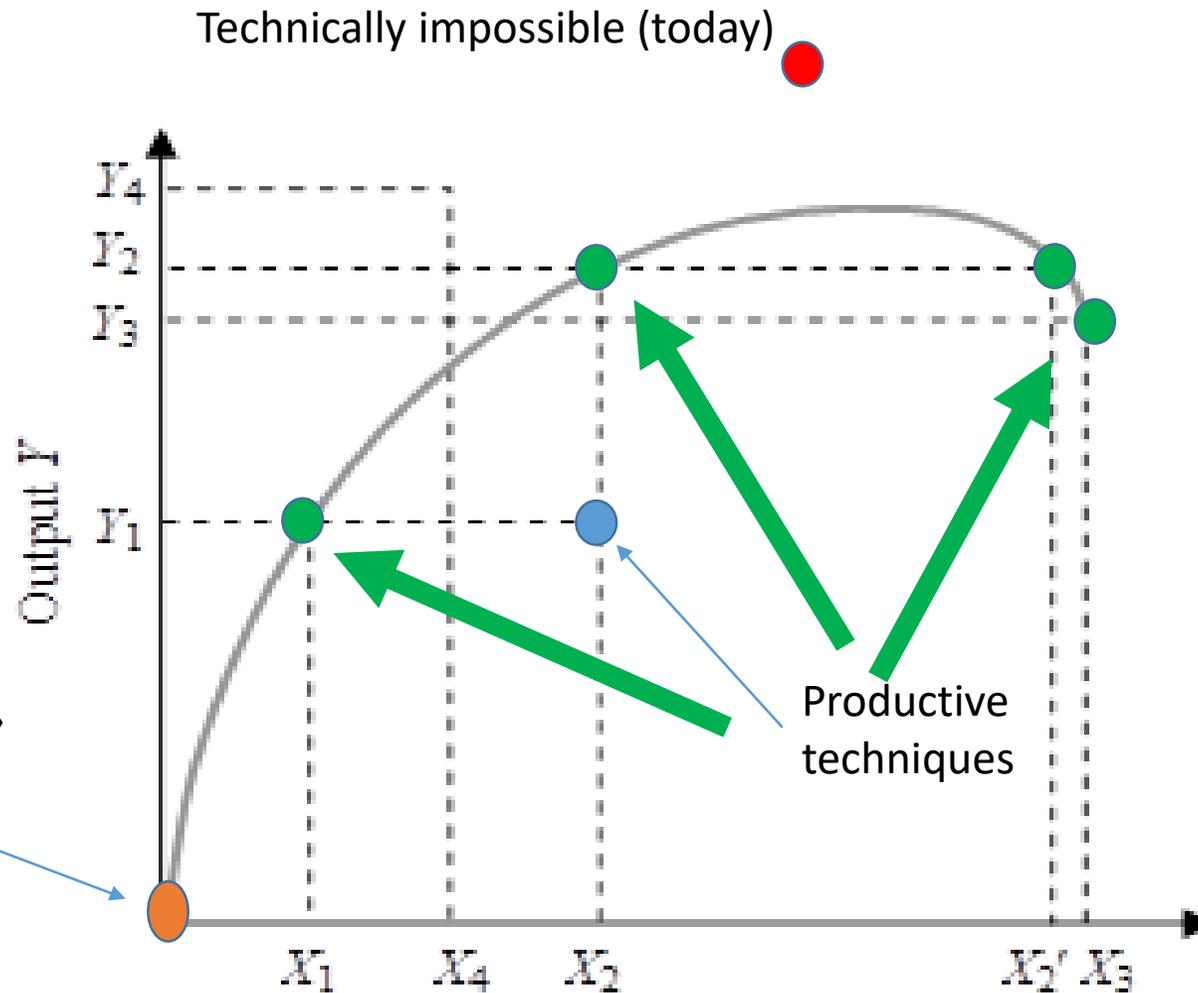
**Technological progress.** We will call technological progress any change which allows the production of a certain quantity of output with a smaller quantity of input, or the production of new higher quantities of output - that were not previously producible - with a given amount of input.

The set of all achievable combinations of outputs and inputs deriving from the available technology ("**productive techniques**") is defined as "**production set**": the **technological constraint**.





# Productive techniques



The «no-land of plenty» assumption.

The perfect divisibility assumption of inputs and outputs.

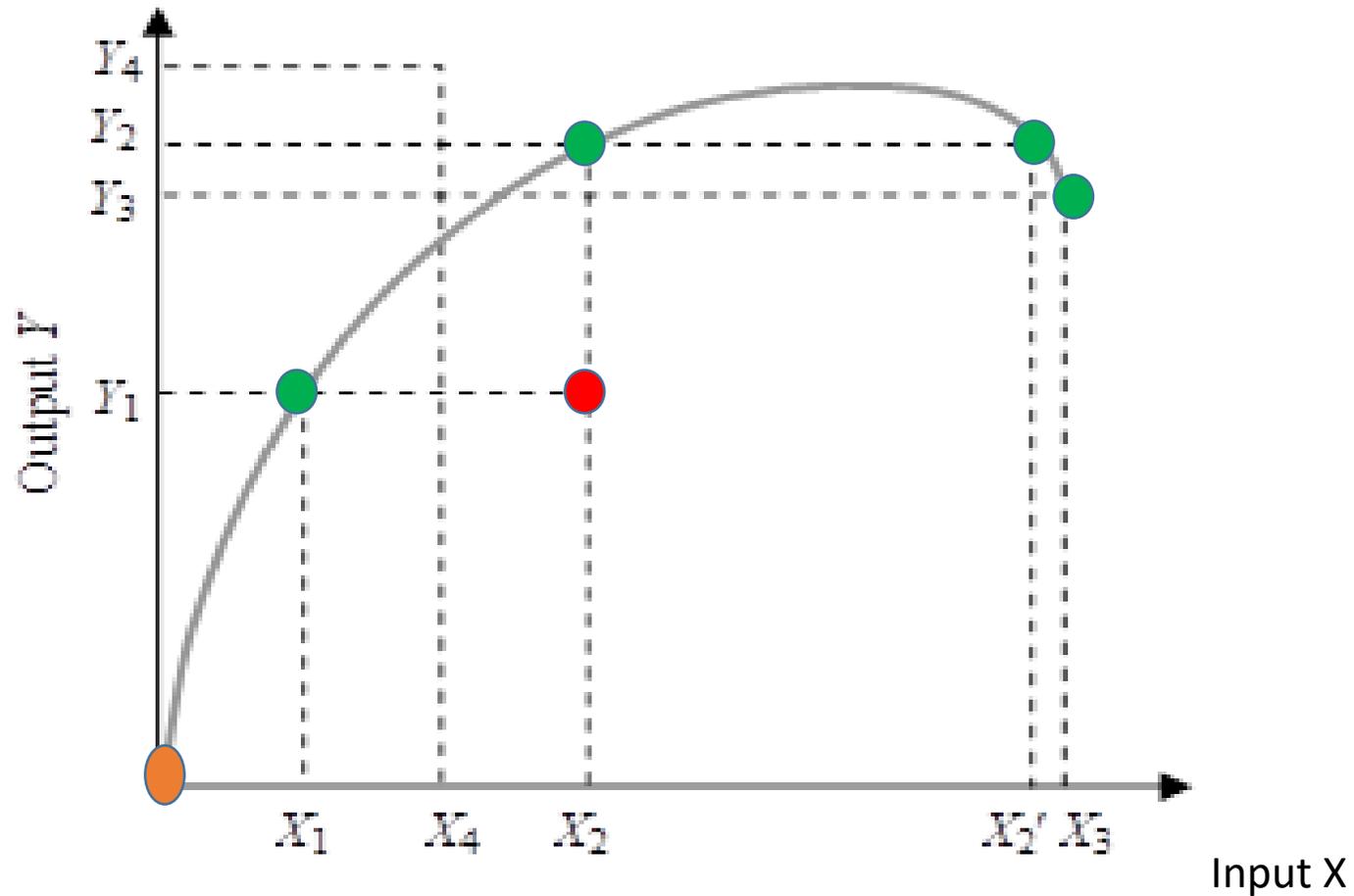
How to produce a given  $Y$ ?  
 $X^*$ ?





# Output-efficiency and the production function

$$Y^{\max} = f(X)$$

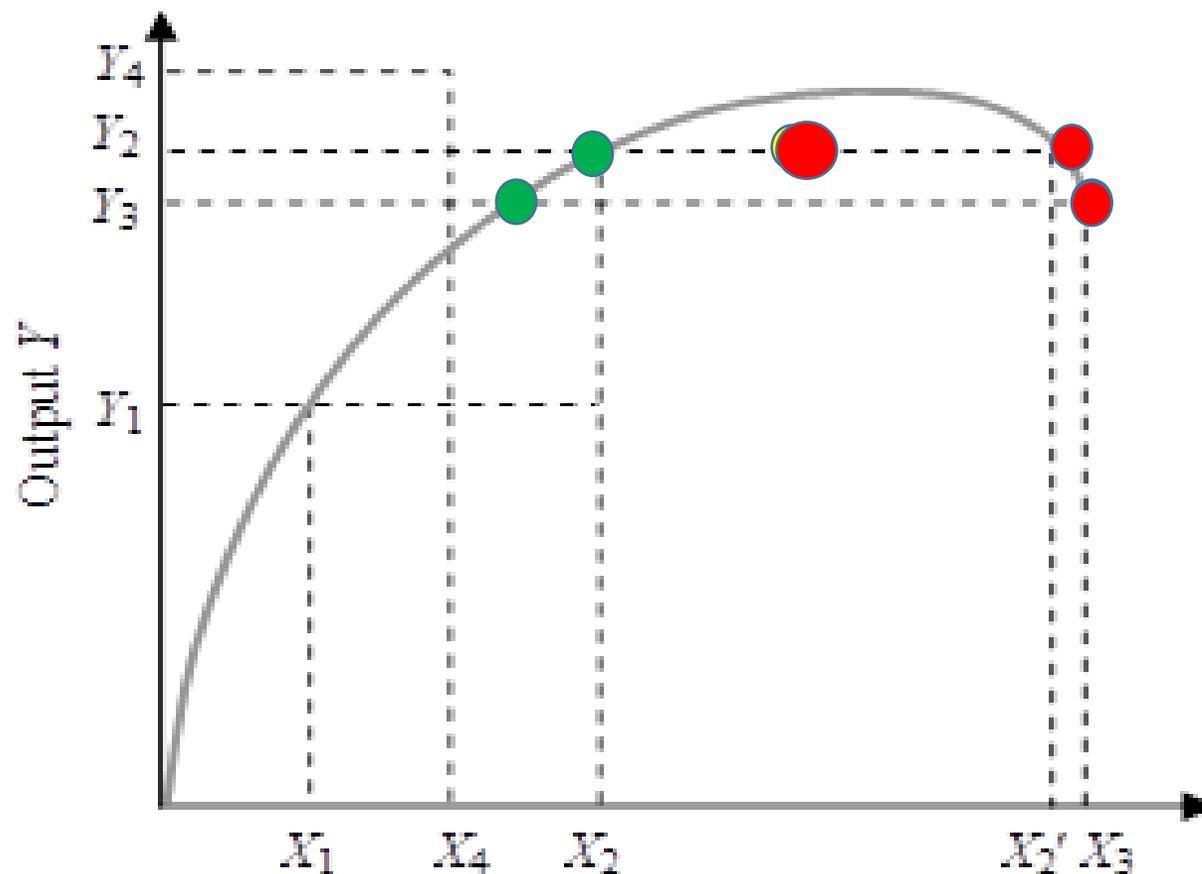




# Interacting with ... cost-cutters

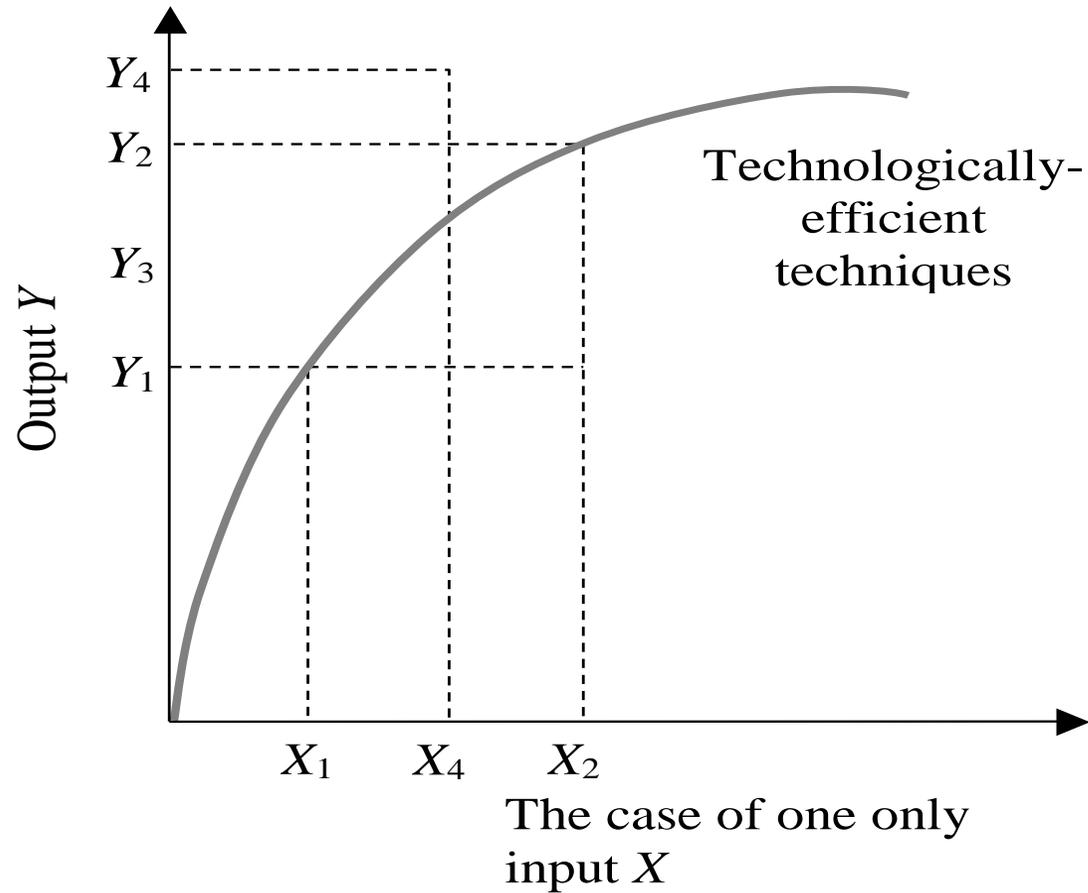


Up in the Air (2009)

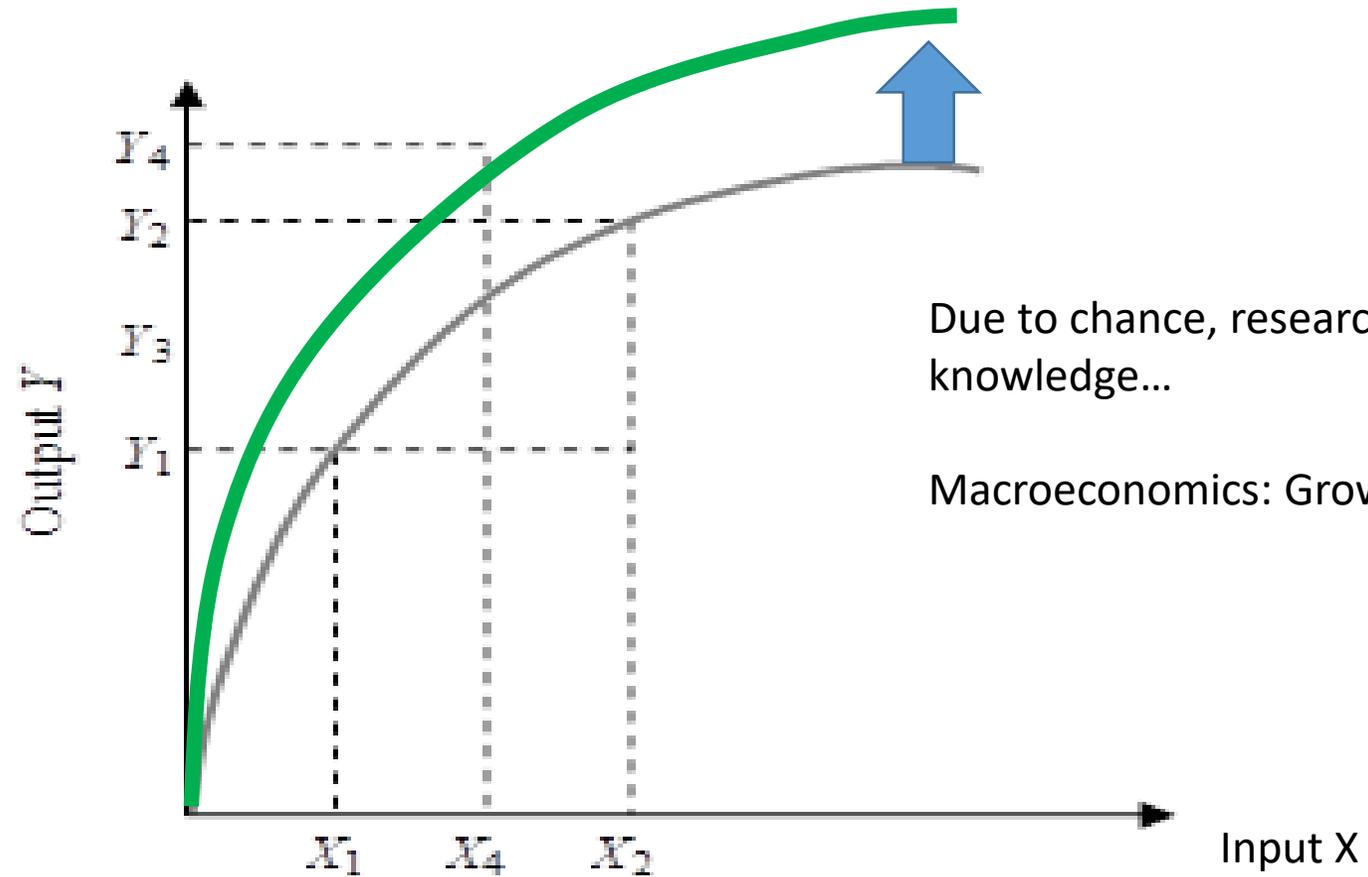




# The technologically efficient productive techniques



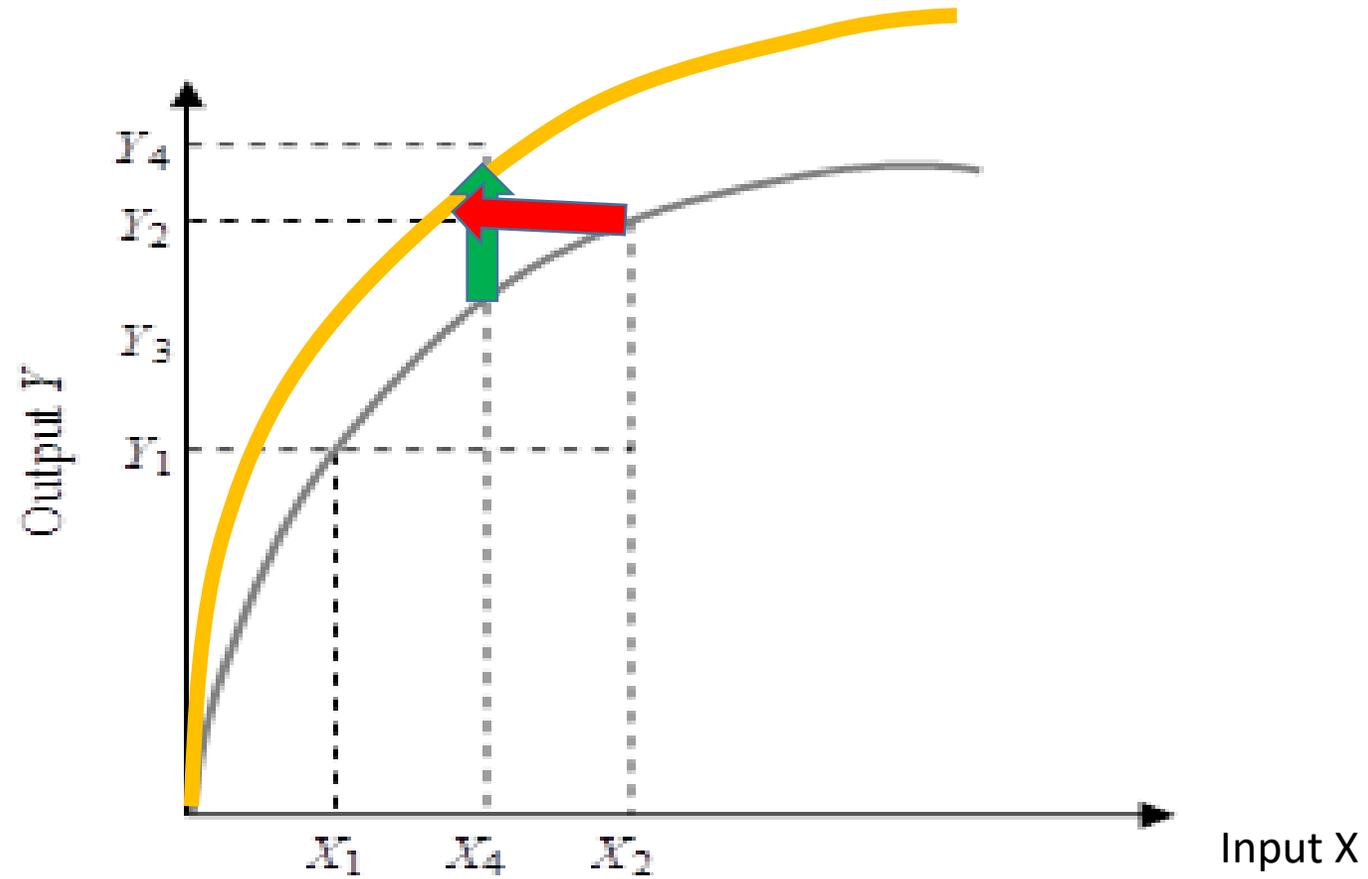
## The 1-input case



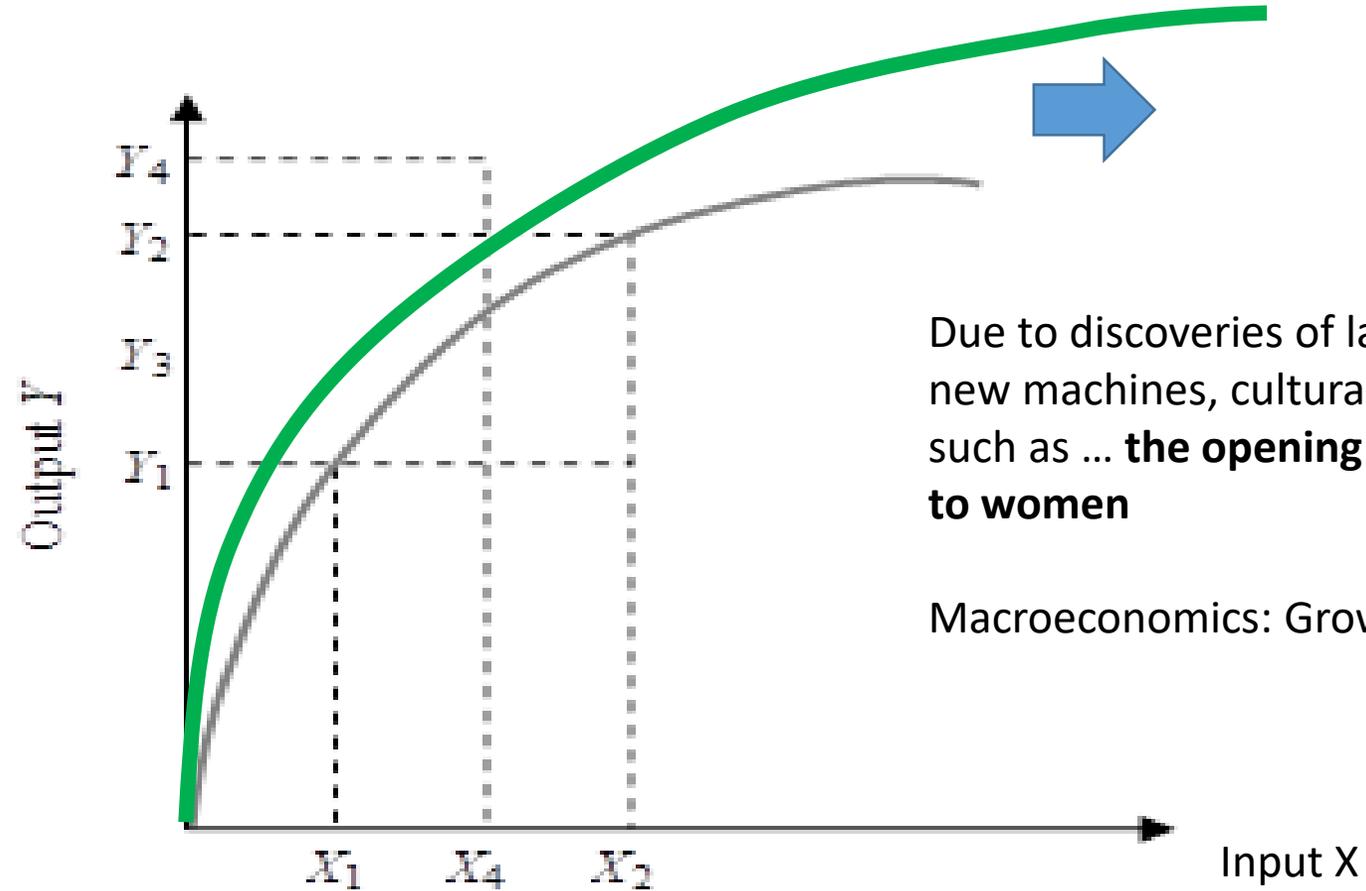


# Technological Progress: the AI debate

Good or bad?



## The 1-input case



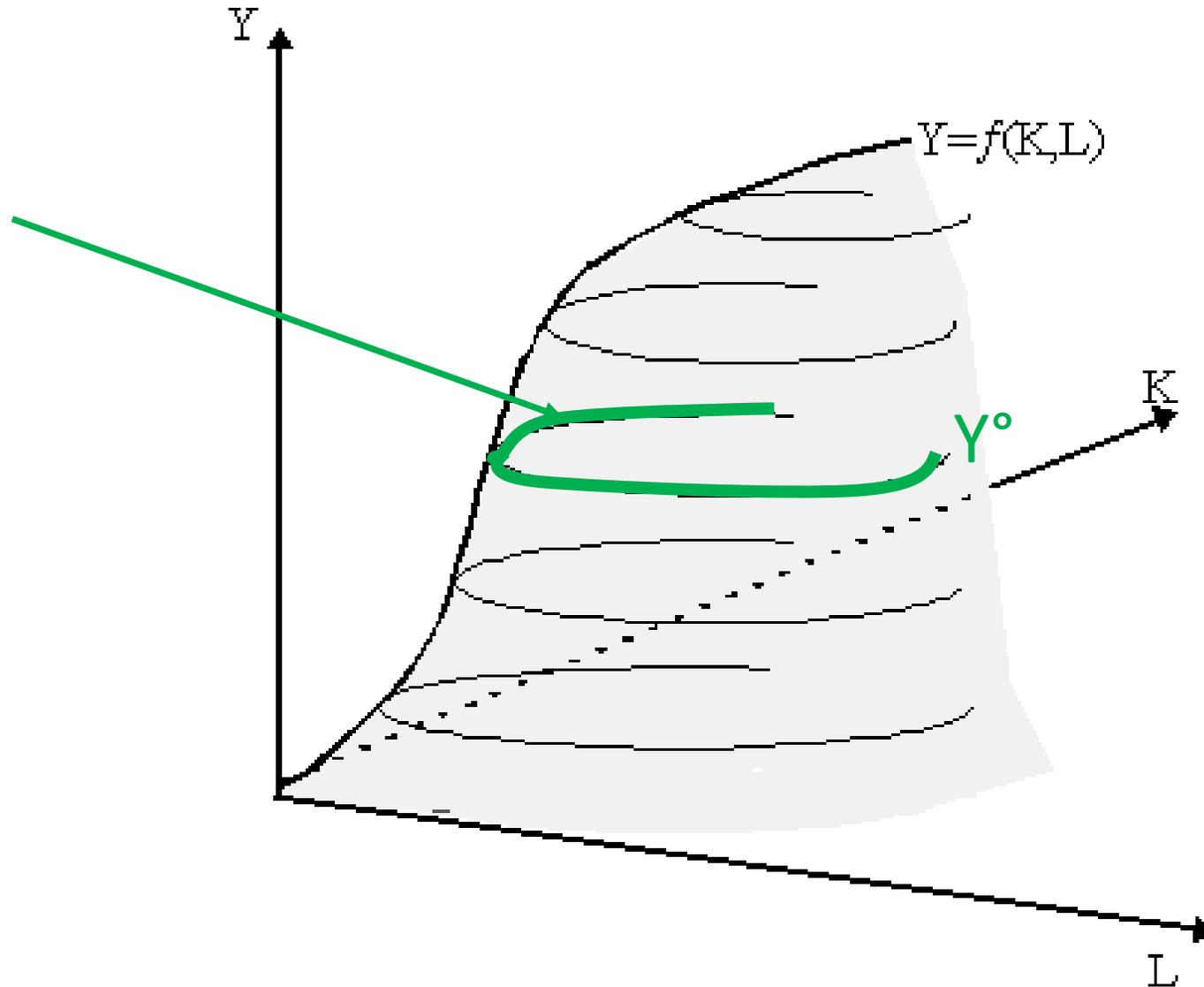
Due to discoveries of land, investment in new machines, cultural changes in society such as ... **the opening of the labor market to women**

Macroeconomics: Growth theory.

# 2 inputs- production function

Level curve:  
 $Y^{\circ} = f(K, L)$

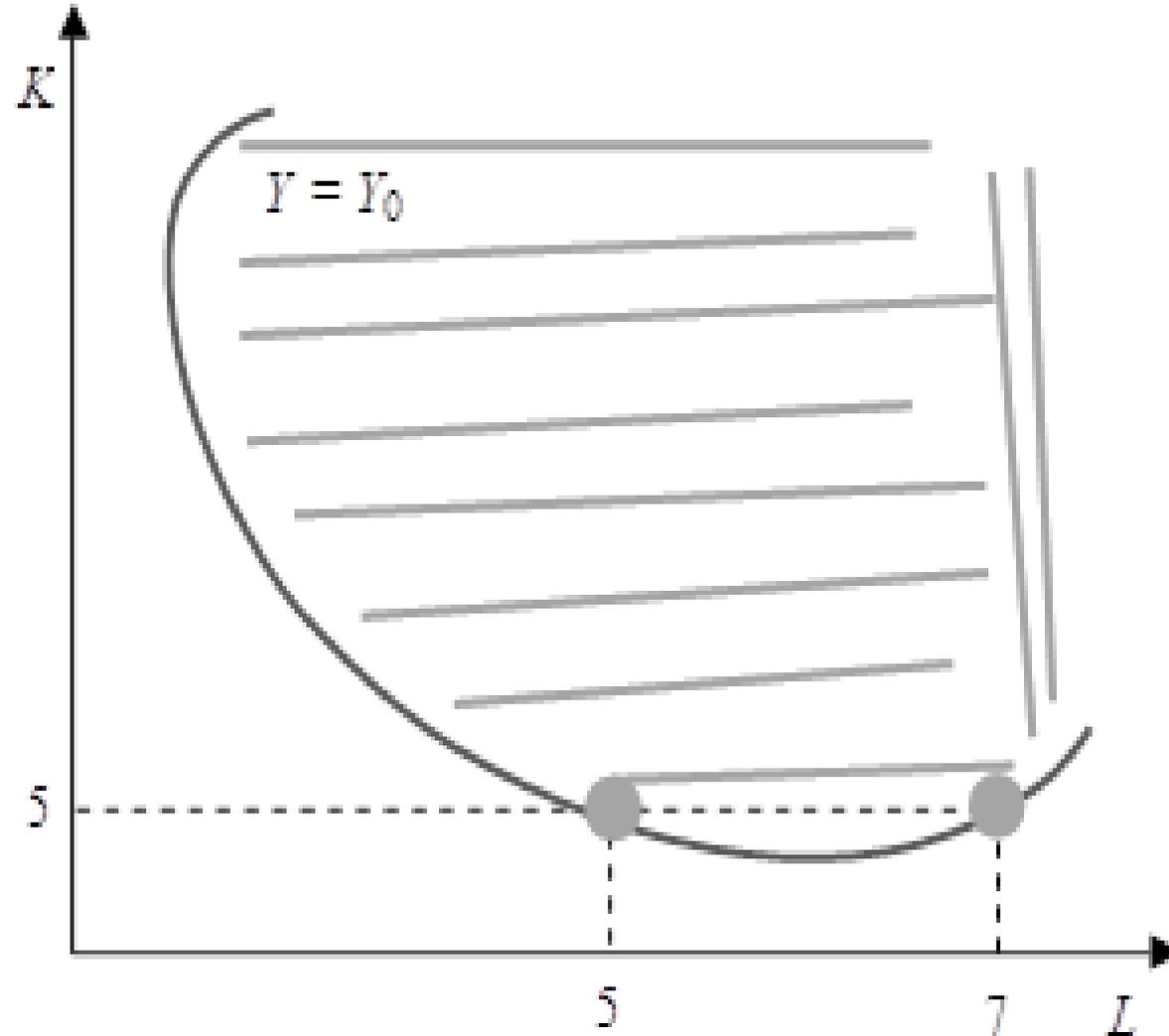
Many (K,L)  
combinations  
guarantee a  
given  $Y^{\circ}$  as  
maximum  
output, not  
one only.



$$Y^{\max} = f(K, L)$$

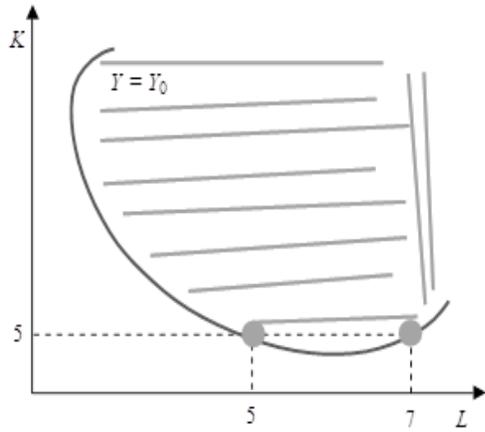


# An Isoquant: an output efficient locus





# Along the Isoquant



$$Y^{\max} = f(K, L)$$

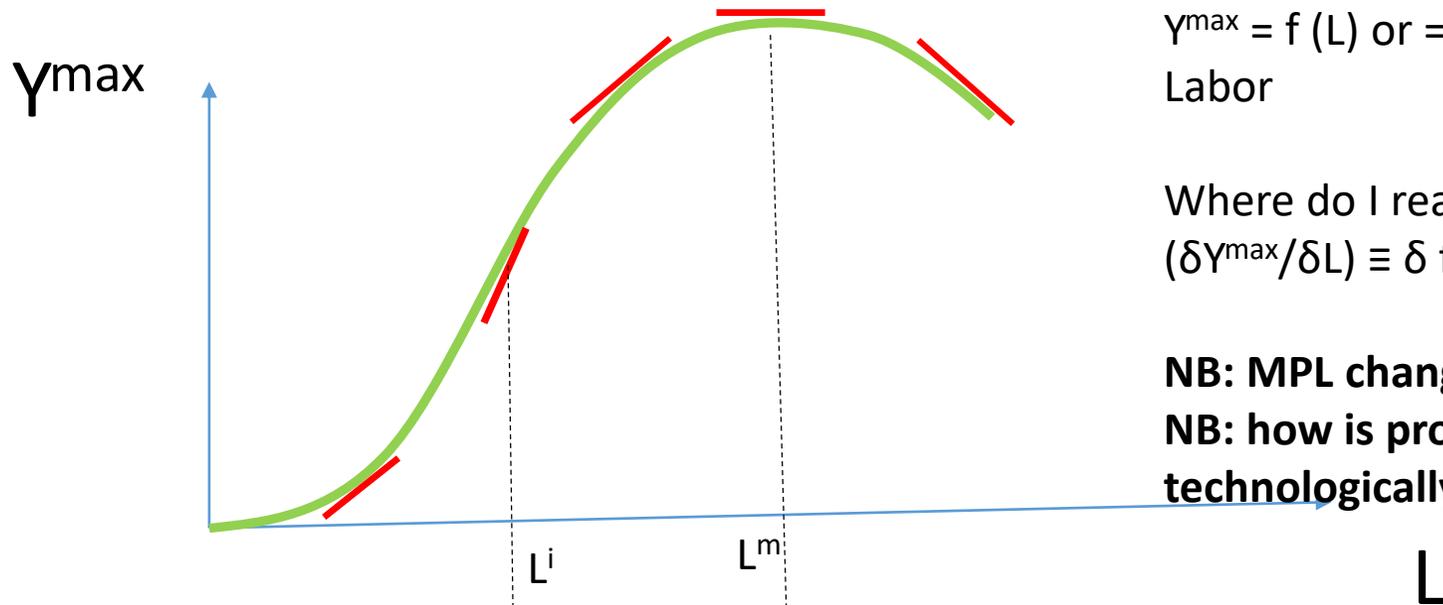
$$Y^{\max} = Y_0 = f(K, L)$$

MARGINAL  
PRODUCTIVITIES  
OF...

$$dY = 0 = dK \times \frac{\partial Y}{\partial K} + dL \times \frac{\partial Y}{\partial L} = f^K dK + f^L dL$$



# Marginal Productivity, the slope of the PF



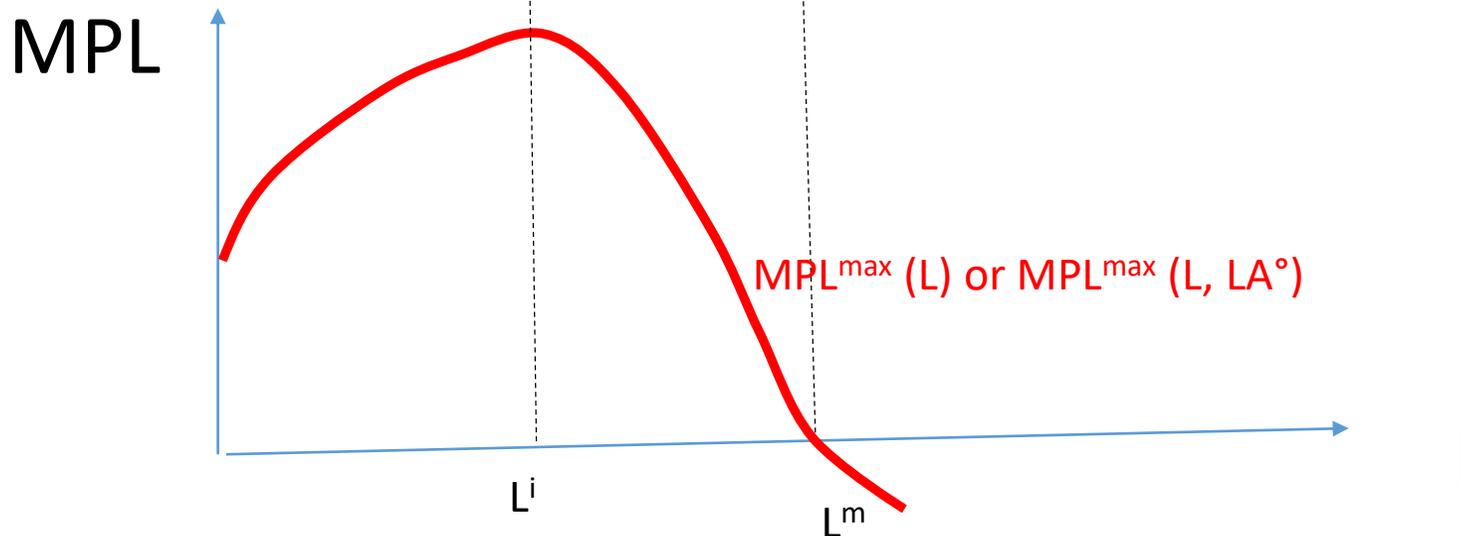
$Y^{\max} = f(L)$  or  $= f(L, LA^{\circ})$  where  $LA$  is Land and  $L$  Labor

Where do I read MPL:

$$(\delta Y^{\max} / \delta L) \equiv \delta f(L) / \delta L \text{ or } \delta f(L, LA^{\circ}) / \delta L ?$$

**NB: MPL changes with L: the MPL function.**

**NB: how is productivity of labor in the technologically inefficient part of the PF?**



Why this shape?

# Some calculations

If  $MPL(13) = 80$  shirts  
and  
 $Y^{\max}(L=13) = 2700$  shirts

$$Y^{\max}(L=14) = ?$$

$$Y^{\max}(L=14) = 2780$$

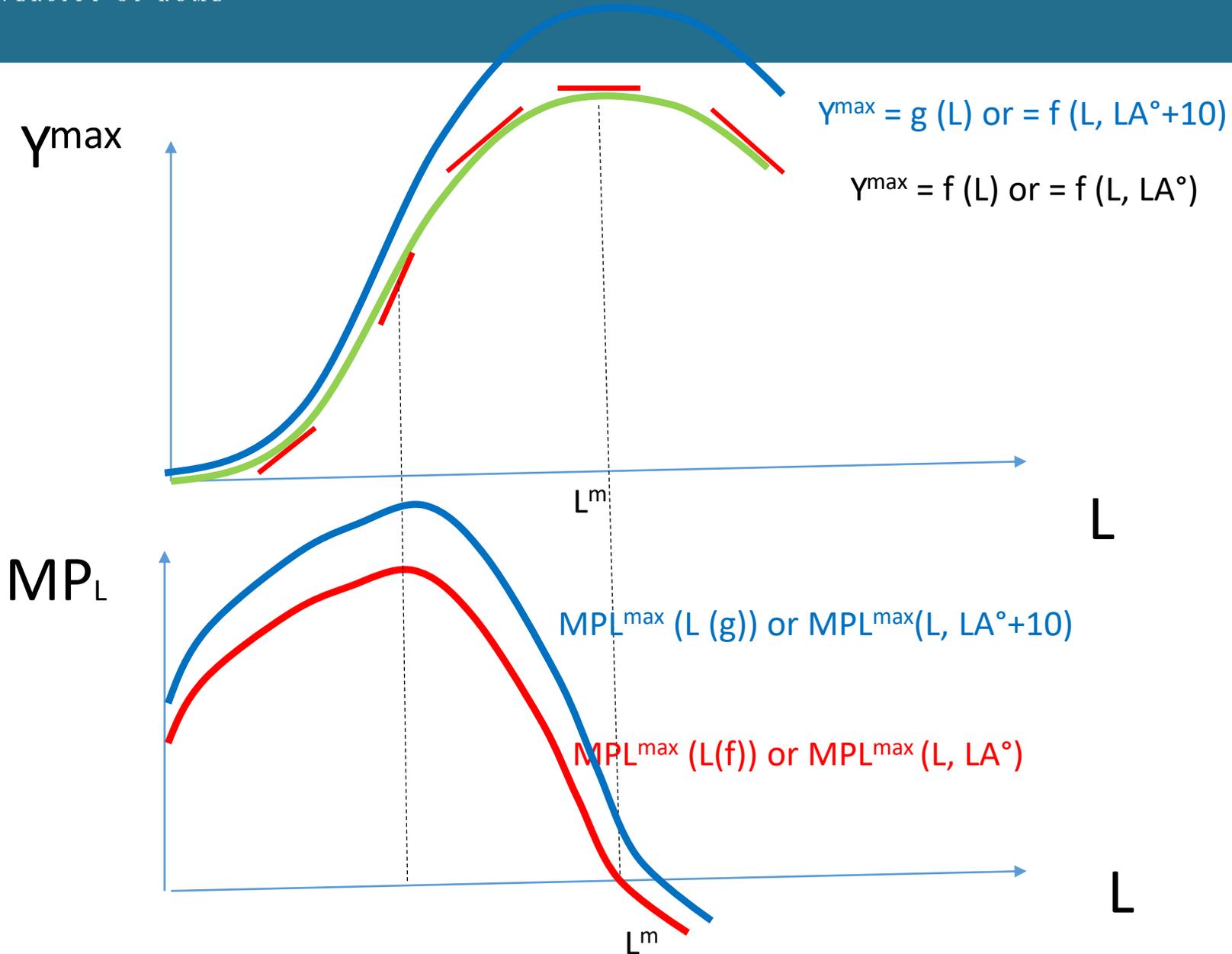
If  $Y^{\max}(L=14) = 2780$  shirts  
and  
 $Y^{\max}(L=15) = 2800$  shirts

Then ...  
 $MPL(14) = ?$

$$MPL(14) = 20 \text{ shirts}$$



# Marginal Productivity and technical progress





$Y/L$  = **Average** Productivity of Labor collapses as L grows?

Let them enter...

Average?

1,50

1,50

1,60

1,55

1,70

1,60

1,80

1,65

1,70

1,66

**1,66**

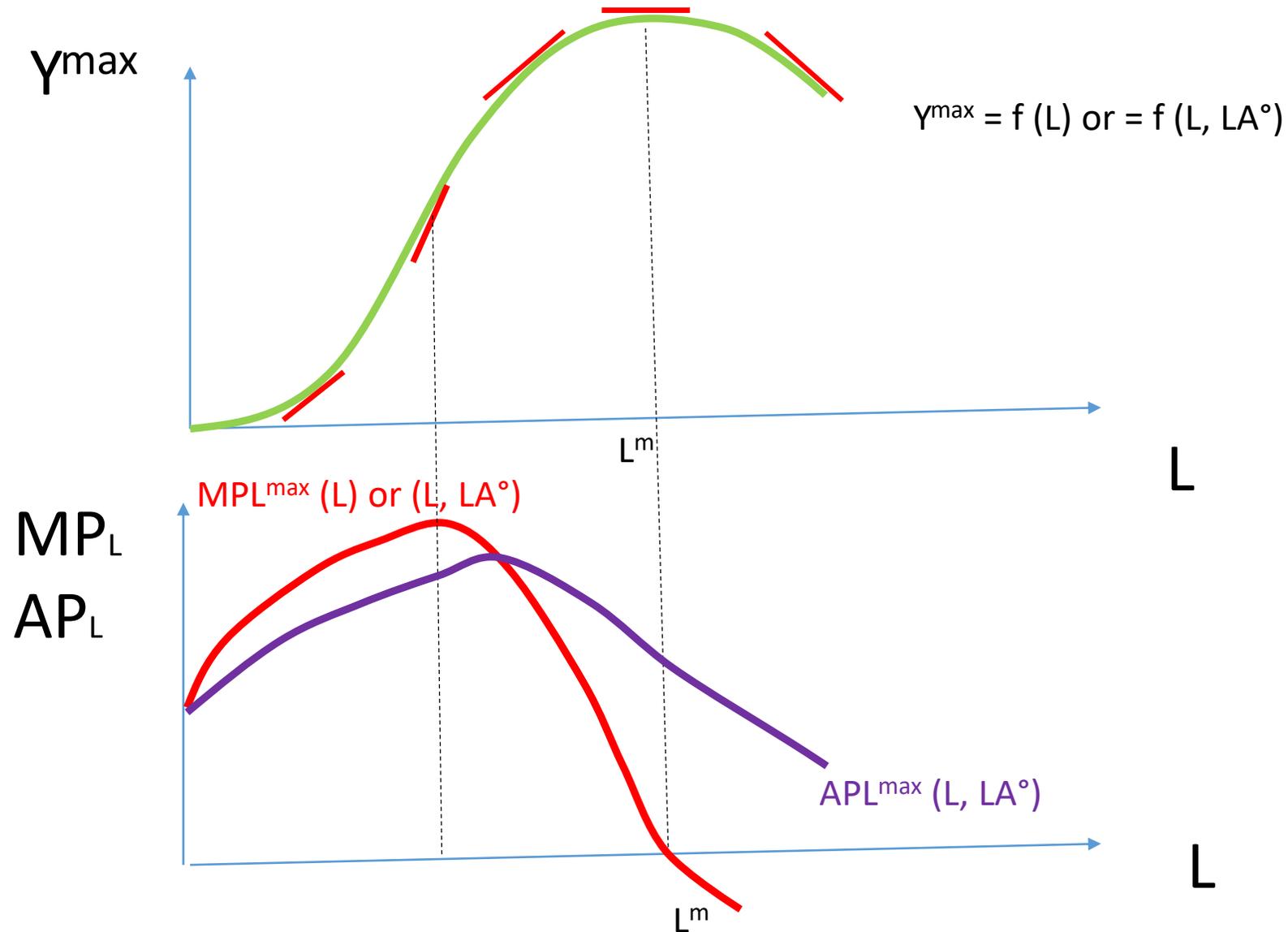
**1,66**

1,50

1,63

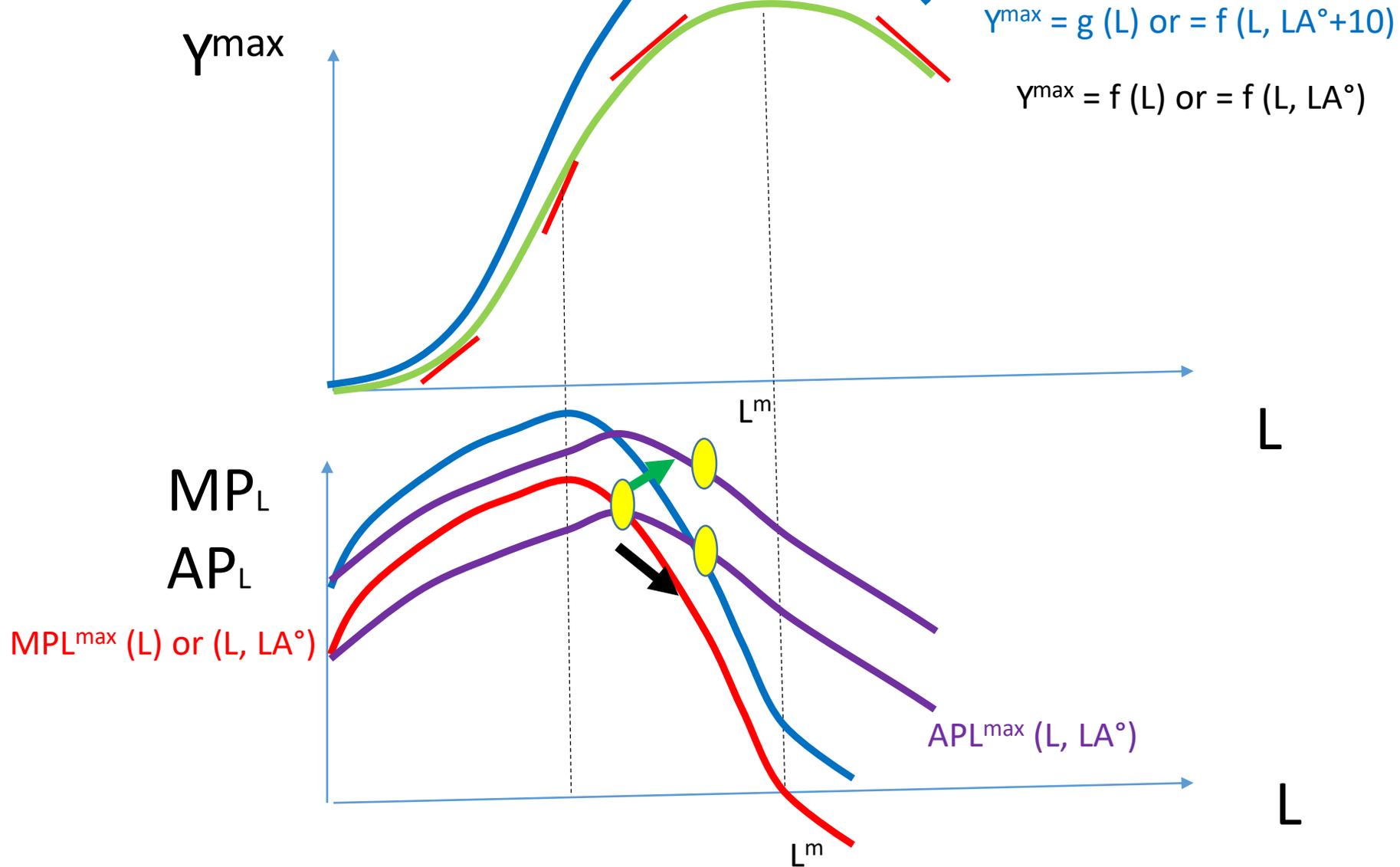


# Average Productivity? A function





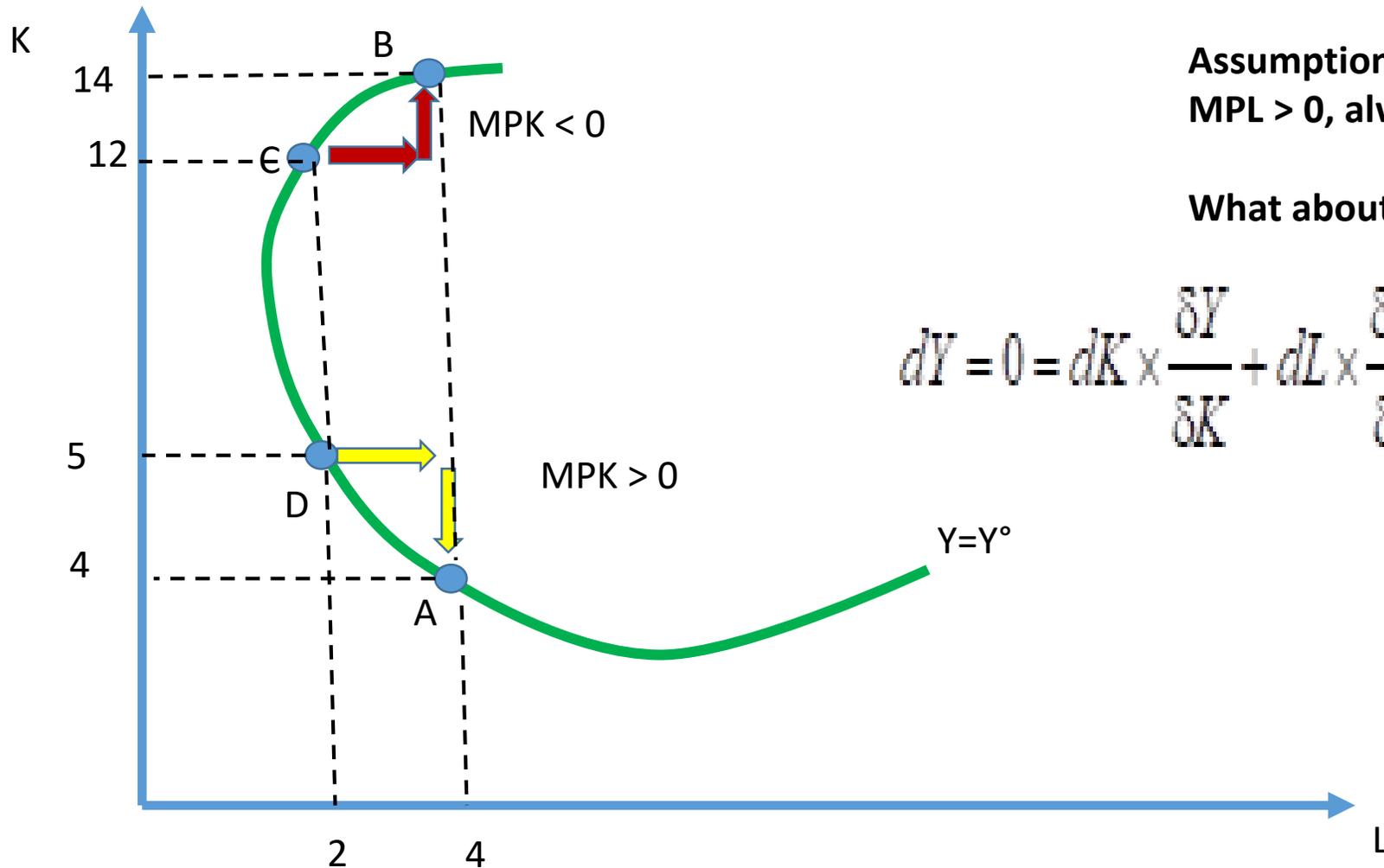
# Malthus: true?



Will technology save us from the demographic Malthusian trap?



# The Isoquant, again



**Assumption:**  
MPL > 0, always

**What about MPK ?**

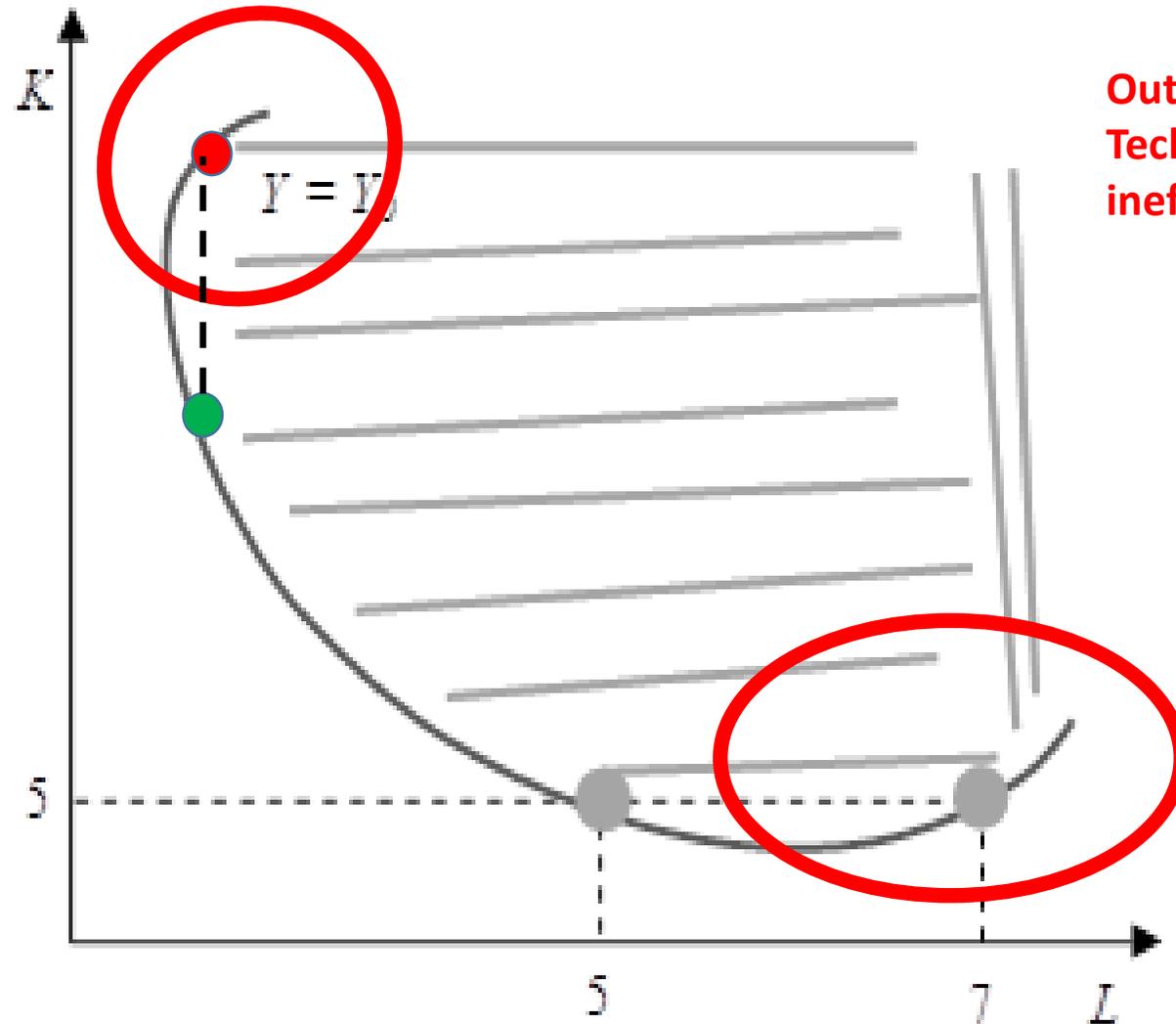
$$dY = 0 = dK \times \frac{\delta Y}{\delta K} + dL \times \frac{\delta Y}{\delta L} = f^k dK + f^l dL$$



# Positively sloped?

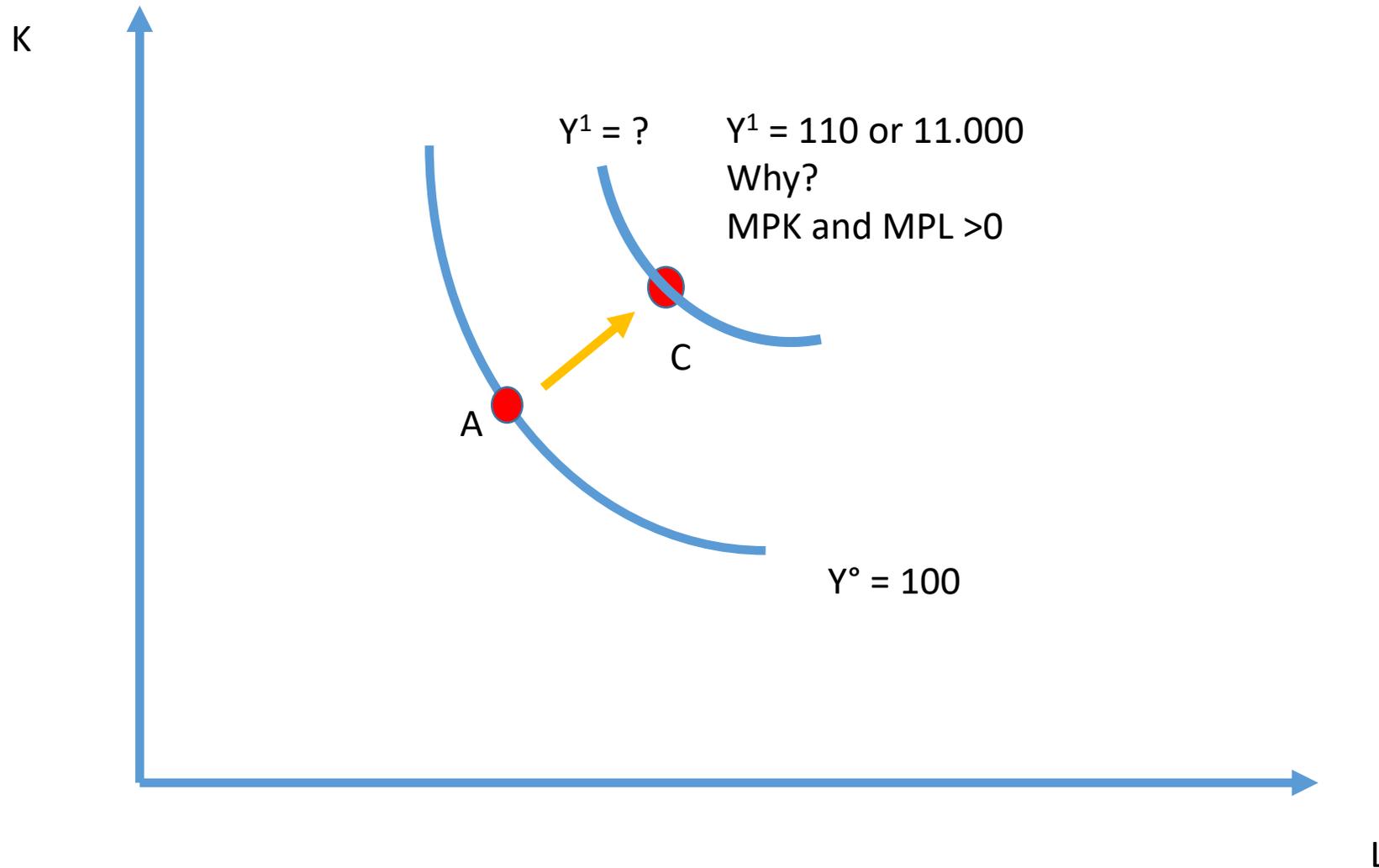
Isoquants are decreasing,  
why?

MPK and MPL > 0!

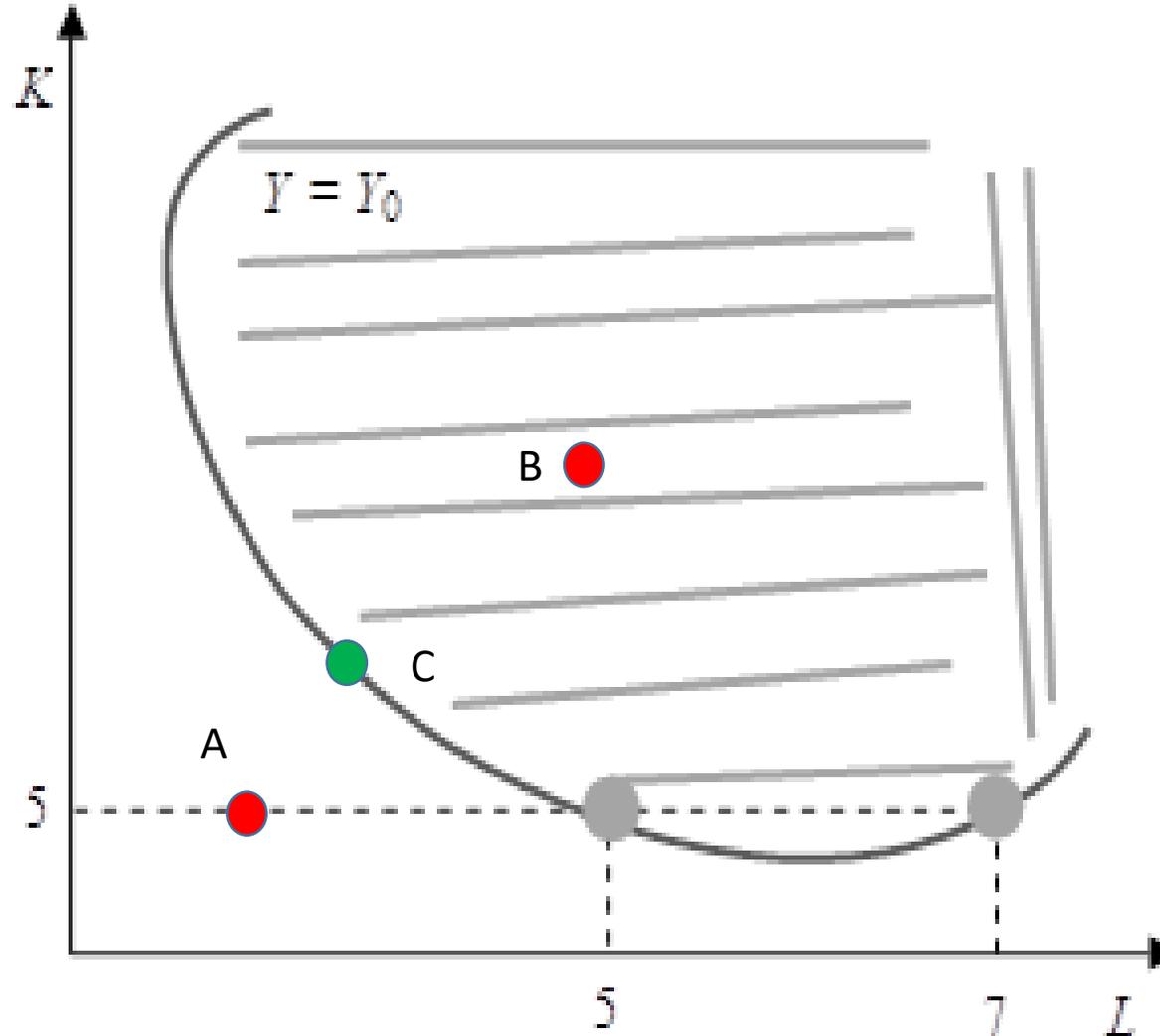


Output efficient,  
Technologically  
inefficient (MPK < 0)!

# Isoquants: implications

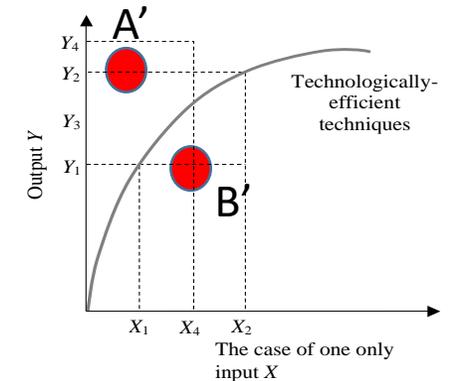


# An Isoquant: an output efficient locus



B: why produce  $Y^\circ$  with so many input?

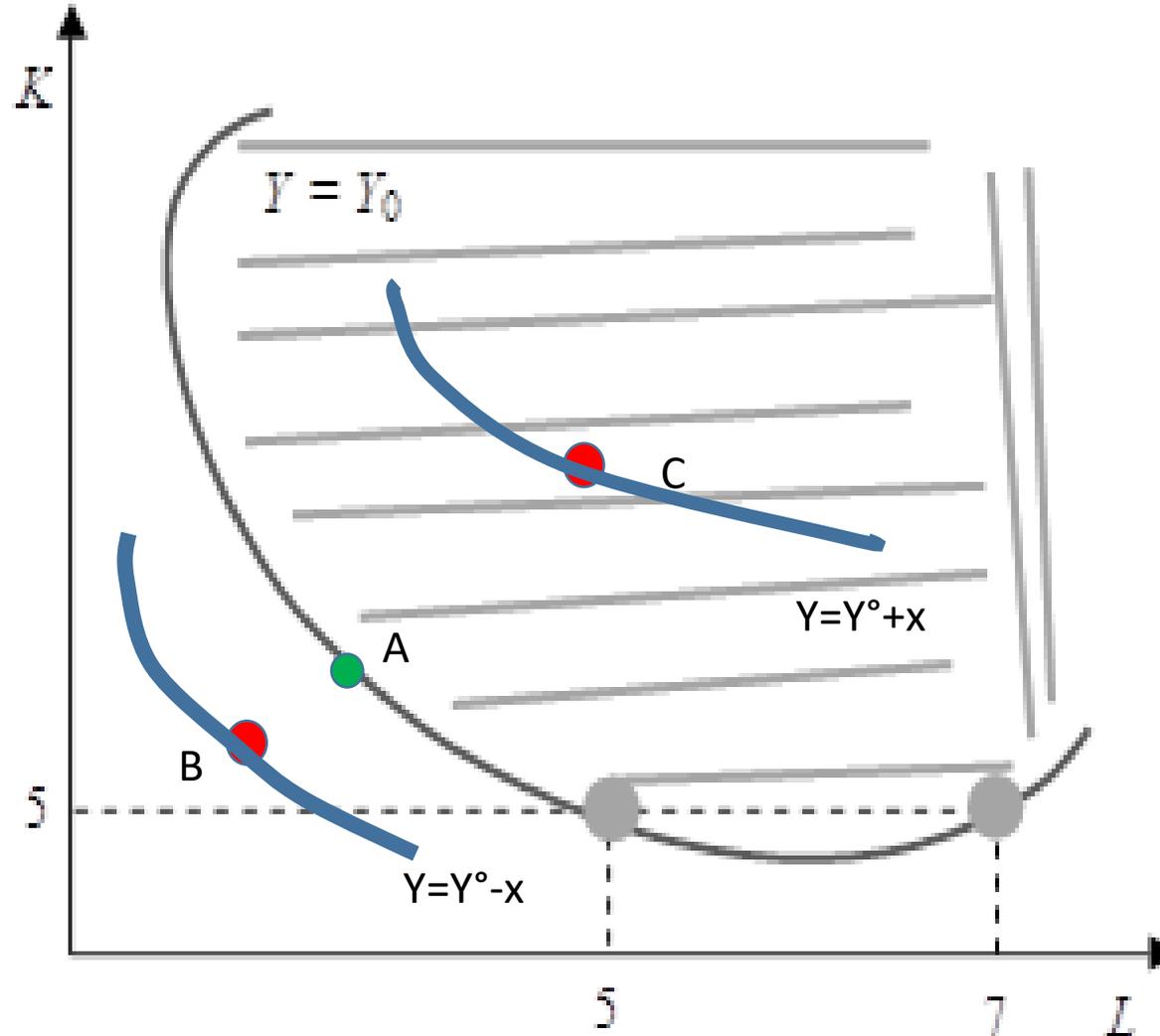
A: impossible to produce  $Y^\circ$  with those input



B': why produce  $Y_1$  with so much input  $X_4$ ?

A': can't produce  $Y_2$  with that input  $X_1$ .

# PS: a further clarification



B: technologically possible  
(for  $Y=Y^0-x$ )

C: output and  
technologically efficient  
(for  $Y=Y^0+x$ )

A: output efficient (and  
technologically efficient)  
for  $Y=Y^0$

B: technologically  
impossible (for  $Y=Y^0$ )

C: output and  
technologically inefficient  
(for  $Y=Y^0$ )

