

**SEVENTH EDITION**

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# **OPTIONS, FUTURES, AND OTHER DERIVATIVES**

**John C. Hull**

*Maple Financial Group Professor of Derivatives and Risk Management  
Joseph L. Rotman School of Management  
University of Toronto*



PEARSON EDUCATION INTERNATIONAL

**Course  
“Derivatives”  
(Academic Year 2015-16)**

The chapters from Hull (2009 – Seventh edition) that match with the program of the course are listed below:

- Chapter 1 – (All)
- Chapter 2 – (All)
- Chapter 3 – (All)
- Chapter 4 – (From 4.1 to 4.7 included)
- Chapter 5 – (All)
- Chapter 6 – (All)
- Chapter 7 – (All)
- Chapter 8 – (From 8.1 to 8.8 included)
- Chapter 9 – (All)
- Chapter 10 – (All)
- Chapter 24 – (All the Exotic Options are included, but only definitions of the derivatives and their possible application are requested. The pricing of these instruments is not part of the program)

In some cases slides will be available on the website for students.

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