

## Part II: Fitting models to empirical Data

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## Fit a model to the data.

```
%how the US Long term Gov Bond yields is trending to estimate the  
future values.
```

```
%create a linear regression model named fitModel1 using d as a  
predictor.
```

```
%(y ~ 1 + x1)  
fitModel1 = fitlm(d,LTGIVeuro)  
% plot data and model fit  
plot(fitModel1)
```

```
fitModel1 =
```

```
Linear regression model:
```

```
y ~ 1 + x1
```

```
Estimated Coefficients:
```

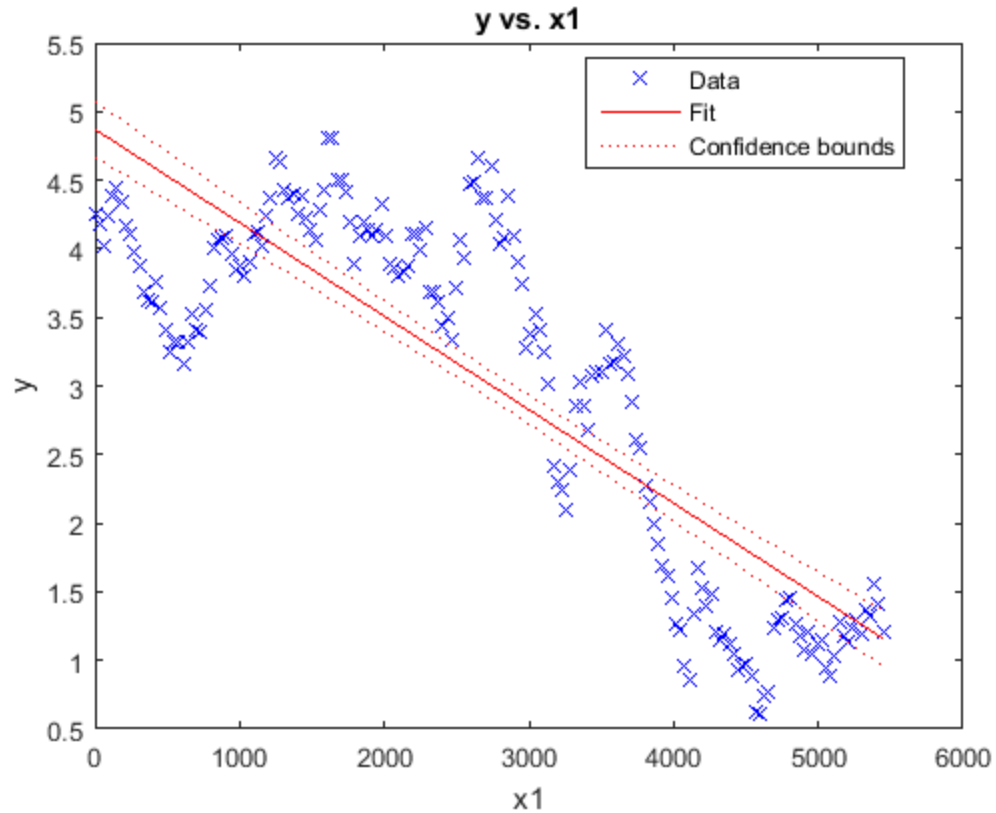
	<i>Estimate</i>	<i>SE</i>	<i>tStat</i>	<i>pValue</i>
	_____	_____	_____	_____
(Intercept)	4.8709	0.10345	47.084	2.1024e-102
x1	-0.00068126	3.2845e-05	-20.742	2.2695e-49

```
Number of observations: 180, Error degrees of freedom: 178
```

```
Root Mean Squared Error: 0.697
```

```
R-squared: 0.707, Adjusted R-Squared 0.706
```

```
F-statistic vs. constant model: 430, p-value = 2.27e-49
```



## Fit a quadratic model to the data.

```
%(y ~ 1 + x1 + x1^2)
fitModel2 = fitlm(d,LTGIVeuro,'quadratic')
plot(fitModel2)
```

```
fitModel2 =
```

Linear regression model:

$$y \sim 1 + x1 + x1^2$$

Estimated Coefficients:

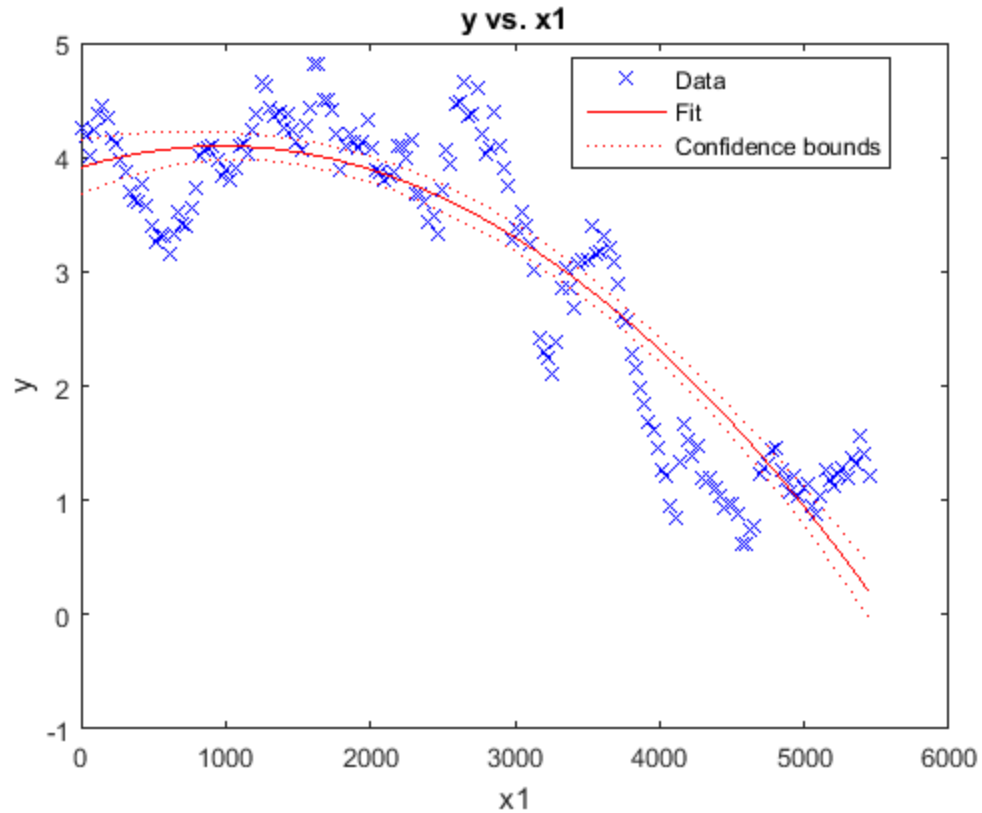
	Estimate	SE	tStat	pValue
(Intercept)	3.9129	0.12016	32.562	1.1795e-76
x1	0.00037994	0.00010192	3.7279	0.00025961
x1^2	-1.9479e-07	1.8108e-08	-10.758	4.3557e-21

Number of observations: 180, Error degrees of freedom: 177

Root Mean Squared Error: 0.543

R-squared: 0.823, Adjusted R-Squared 0.821

F-statistic vs. constant model: 412, p-value = 2.73e-67



## Fit a polynomial of degree 3 to data.

```
%(y ~ 1 + x1 + x1^2 + x1^3)
fitModel3 = fitlm(d,LTGIVeuro,'poly3')
plot(fitModel3)
```

```
fitModel3 =
```

Linear regression model:

$$y \sim 1 + x1 + x1^2 + x1^3$$

Estimated Coefficients:

	Estimate	SE	tStat	pValue
(Intercept)	3.2927	0.14213	23.167	2.4422e-55
x1	0.0017655	0.00022658	7.7919	5.5045e-13
x1^2	-8.324e-07	9.6801e-08	-8.5991	4.2879e-15
x1^3	7.8025e-11	1.1678e-11	6.6812	3.0025e-10

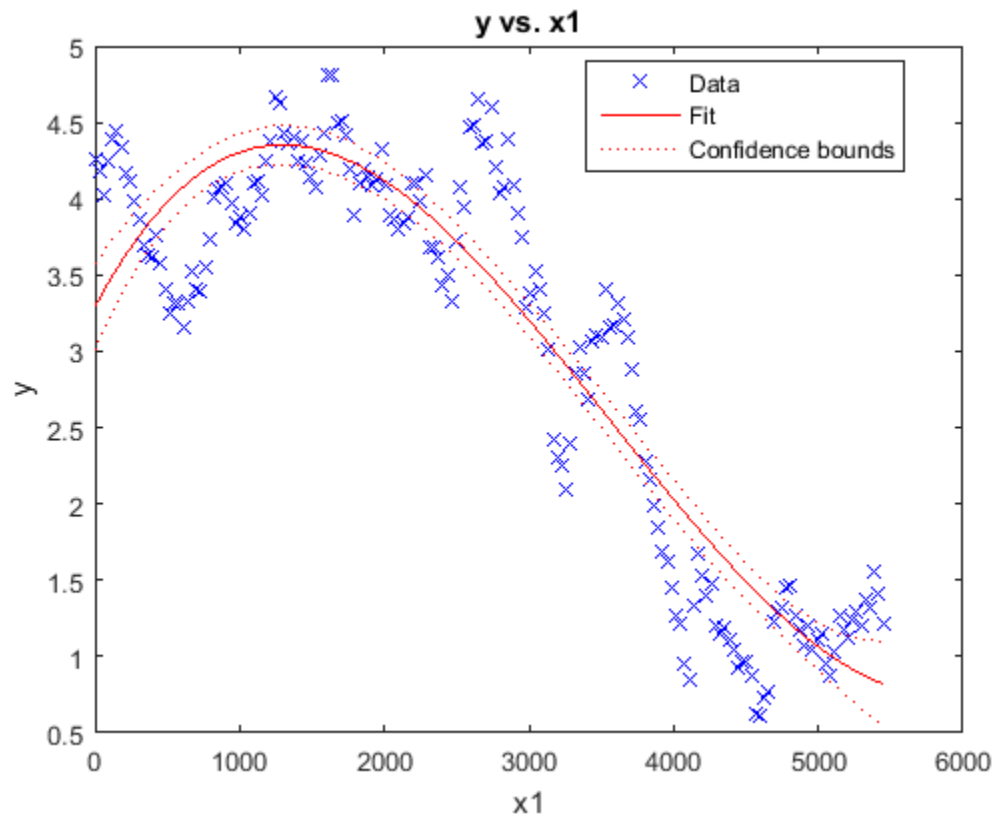
Number of observations: 180, Error degrees of freedom: 176

Root Mean Squared Error: 0.487

R-squared: 0.859, Adjusted R-Squared 0.856

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*F*-statistic vs. constant model: 357, *p*-value = 1.47e-74



## View information about the fit

```
info1= fitModel1.Coefficients
info2= fitModel2.Coefficients
info3= fitModel3.Coefficients
```

```
info1R2 = fitModel1.Rsquared
info2R2 = fitModel2.Rsquared
info3R2 = fitModel3.Rsquared
```

```
info1 =
```

	<i>Estimate</i>	<i>SE</i>	<i>tStat</i>	<i>pValue</i>
(Intercept)	4.8709	0.10345	47.084	2.1024e-102
x1	-0.00068126	3.2845e-05	-20.742	2.2695e-49

```
info2 =
```

<i>Estimate</i>	<i>SE</i>	<i>tStat</i>	<i>pValue</i>
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(Intercept)	3.9129	0.12016	32.562	1.1795e-76
x1	0.00037994	0.00010192	3.7279	0.00025961
x1^2	-1.9479e-07	1.8108e-08	-10.758	4.3557e-21

info3 =

	<i>Estimate</i>	<i>SE</i>	<i>tStat</i>	<i>pValue</i>
(Intercept)	3.2927	0.14213	23.167	2.4422e-55
x1	0.0017655	0.00022658	7.7919	5.5045e-13
x1^2	-8.324e-07	9.6801e-08	-8.5991	4.2879e-15
x1^3	7.8025e-11	1.1678e-11	6.6812	3.0025e-10

info1R2 =

Ordinary: 0.7073  
Adjusted: 0.7057

info2R2 =

Ordinary: 0.8230  
Adjusted: 0.8210

info3R2 =

Ordinary: 0.8588  
Adjusted: 0.8564

## Predict LT Gov Bond Yields Euro Area for the first 100 days

using fitModel1 and assign the result to ypred1.

```
plot(d,fitModel1.Fitted,'g')
```

```
% use predict function to predict the reponse values given any  
predictor values.
```

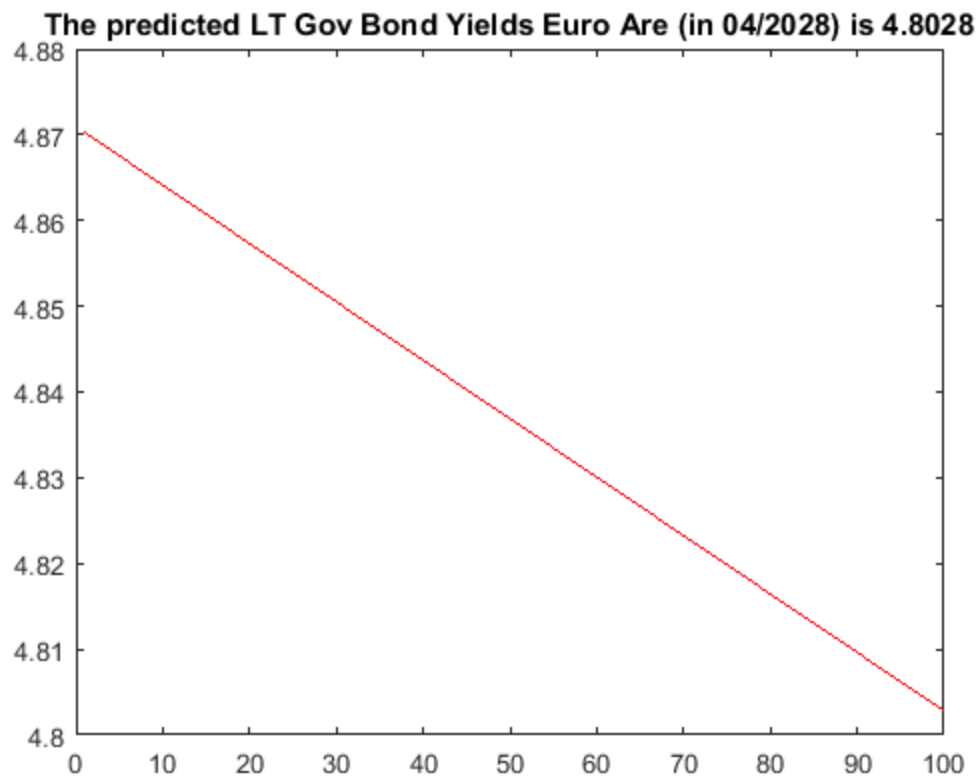
```
ypred1 = predict(fitModel1,(1:100)');
```

```
% plot the predicted  
plot(1:100,ypred1,'r')
```

```
% Extract and report  
rate100 = ypred1(end);
```

---

```
title(['The predicted LT Gov Bond Yields Euro Are (in 04/2028) is  
' ,num2str(rate100)])
```



## Evaluate goodness of fit

plots a histogram of the residuals. the distribution of the residuals of a fit.

```
plotResiduals(fitModel1)
```

```
%Diagnostic plots help you to identify outliers and see other problems  
in
```

```
%your model or fit
```

```
plotDiagnostics(fitModel1, 'cookd')
```

```
% use predict function with the quadratic model
```

```
ypred2 = predict(fitModel2,(1:100)');
```

```
% use predict function with polynomial of degree 3
```

```
ypred3 = predict(fitModel3,(1:100)');
```



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