Exercises 3/5 francesco.dotto@uniroma3.it

Exercise 1

For the population of individuals who own an iPhone, suppose p = 0.25 is the proportion that has a given app.

- 1. For a random sample of size n = 4, find the mean and the standard deviation of the sampling distribution of the sample proportion.
- 2. Find the probability that the proportion of having the app is at least 0.75 when n = 4. [Hint: first, find x.].
- 3. For a random sample of size n = 150, find the mean and the standard deviation of the sampling distribution of the sample proportion.
- 4. Summarize the effect of the sample size on the standard deviation of the sampling distribution of the sample proportion.
- 5. Describe the shape of the sampling distribution of the sample proportion when n = 150.
- 6. Find the probability that the proportion of having the app is at least 0.75 when n = 150.

Exercise 2

You are studying for taking the final exam in Statistics. Based on your preparation, for any given question you think you have a probability of p = 0.70 of getting the correct answer. An exam consists of 60 multiple-choice questions. Consider the sampling distribution of the sample proportion of the 60 questions on which you get the correct answer.

- 1. Find the mean and the standard deviation of the sampling distribution of this proportion.
- 2. What do you expect for the shape of the sampling distribution? Motivate your answer.
- 3. If truly p = 0.70, would be very surprising if you got correct answers on only 60% of the questions? Justify your answer by using the normal distribution to approximate the probability of a sample proportion of 0.60 or less.

Exercise 3

The distribution of profit per year of a restaurant is approximately normal with a mean of 65 (in thousands of dollars) and a variance of 225.

- 1. Compute the probability that a randomly selected restaurant has a year profit greater than 70.
- 2. Compute the probability that a randomly selected restaurant has a year profit less than 50.
- 3. Find the first quartile of the profit per year.
- 4. Find the median of the profit per year.
- 5. Given a sample of 15 restaurants, find the mean and the standard deviation of the sampling distribution for the sample maean.
- 6. Describe the shape of the sampling distribution of the sample mean.
- 7. Compute the probability that in a sample of 15 restaurants, the average for the year profit is between 55 and 75.

Exercise 4

The GPA of 100 randomly selected students among all those graduating from Tor Vergata in 2015 had a median of 2, mean of 3.22, and standard deviation of 0.26.

- 1. Compute the probability that a randomly selected GPA from the population is between 2.5 and 3.5. [Note that the population standard deviation is 2.6.]
- 2. Find the GPA score that is the 82th percentile.
- 3. Find the interquartile range (IQR) of the GPA.
- 4. What is the point estimate of the population mean?
- 5. Is the estimator used in (4) unbiased?
- 6. Compute the probability that the sample mean of GPA is between 2.5 and 3.5.
- 7. Find the GPA score of the sampling distribution that is the 82th percentile.
- 8. Find the interquartile range (IQR) of the sampling distribution of the sample mean.